

I. INTRODUCTION

Sensors bridge the gap between environment under test/observation and the actual measurement. They constitute the most important part of outputs of interest in the environment. Inaccurate and improperly used sensor readings will result in problematic determination and inappropriate subsequent estimation of agent state and decisions in the environment [1].

A generalized data fusion combines data of multiple sources in order to achieve inferences. For instance, while a fighter is unable to see around corners or through a tree-dense area [2], additional senses can provide advanced alarm. Similarly, it may not be possible to determine the quality of one kind of food based merely on the sense of taste, but edibility may be arrived at using a combination of vision and smell. Multi-sensor data fusion is naturally performed by animals and humans to gain more accurate evaluation of the surroundings and especially identifying threats, where the objective is increasing their chances of survival [3].

Measurement data may be merged (fused) at different levels, at observation level; and at the decision level. Raw sensor data can be directly combined by similarity if the sensor data are homogenous [3]. There also has been increasing interest in making distributed sensor-based security systems. It is essential to understand how moving objects interact with each other and the environment to extract the major parameters for the development of automated situational awareness system [4]. In addition to the issue of automated situational awareness, privacy protection is another important issue in surveillance. It is very desirable for a surveillance system to recognize human activities.

Successful implementations of many commercial and military applications require timely, reliable, and precise information to support decisions for remote security operations. Developing effective security monitoring mechanisms to provide situation awareness has become an increasingly important focus. Thus, relying on raw sensor data is extremely challenging primarily because security events evolve continuously and security space information is usually incomplete and noisy. Some dynamic security monitoring systems combine a number of different techniques to data collected from distributed sensors like intrusion detection based on fusing decisions and information correlation to compute event indicators [5].

This paper presents a methodology for multi-sensor based analysis of a surrounding of a highly valuable asset. This is an essential part of a decision making system of a security system [6].

Multi-Sensor based networks are an emerging technology that promises ability to monitor the physical world. The aim of the work in this paper is to be able to estimate (predict) the next security status of a moving object (agent) in an indoor monitored space and be able to make a decision on the system status at any given time t .

II. SENSOR TYPES

This proposed system utilizes three types of sensors to accomplish its goal. Sonar sensor [7] to scan space for total number of moving agents, laser sensor [8, 9] to measure speed of agent and finally radio frequency sensor [10, 11] to provide the system with agent identification.

Sonar sensors are mainly categorized into propagation and distance types. The LV MaxSonar-EZ0 [7] is one type of those sensors that can be utilized for such application capable to cover up to 645.16 centimeters of distance and makes a reading every 50msec and its cone diameter is wide enough to completely cover the floor part of the area of interest. This set of sensors is responsible to report the total number of the existing agents in the area under surveillance.

On the other side laser sensors [8, 9] are also grouped under two major types that are displacement and position. The CSI-430 [8] sensor is capable to capture moving agent's speed up to 9.144 meters away and it provides the system with resolution feedback with a reading that is 5 digits.

Finally, Radio Frequency sensors [10, 11] utilize radio waves propagation to transfer data. The Tag-it HF-I [10] sensor set that is equipped with 13.56 MHZ transponders could be used to acquire and report the access right of any agent that enters the space of interest.

III. A MONITORING SYSTEM

In a target monitoring applications; multi-sensor data usually transferred to measurements of angular direction and range which in turn fed into a predictor to estimate the target's next position and velocity (system states) utilizing observations from different attributes and analyzing the motion type of the target with respect to a reference point, helps in making a decision of the intent of the target (e.g., flag and alarm or no-flag needed). The determination of the target's next position and velocity from a noisy time-series of sensor data forms a typical estimation problem where Kalman filtering techniques fits better [3].

This paper proposes a new monitoring system model utilized to predict the next state of moving agent(s) in a closed space as in Fig.1 by fusing information from multiple sensors of different types.

The area under surveillance is divided into four zones A, B, C and D shown in Fig.1 where each is only a ring with a width that is wide enough to be completely covered by the sonar sensor's cone's diameter. This sensor could be mounted in the middle of the ceiling of each ring and be able to provide a total number of agents at any given time in any zone [6, 7]. As shown in Fig.2 the model also reads in data from a grid of laser sensors [6, 8, 9] to capture agent speed. The following laser sensor network was assumed; four sensors in the X direction and another set of four laser sensors in the Y direction with each of them reporting the agent(s) speed in feet per second as in Fig.2.

Finally an identification data transmitter is associated with each agent and captured by RF Radio Frequency sensor [10, 11] to support the system with an ID of any moving agent. For sake of simplicity, radio frequency sensor will provide three pre-defined types of agent's access rights ("Trusted", "Semi-Trusted" and "Unknown"). Laser and sonar sensor data sets will then be fed into a sensor similarity processing sub-system that will be responsible to filter out any noisy sensor input of each sensor-type and come up with a single reading based on sensor similarity method. After sensor data have been filtered, speed on X-axis and Y-axis outputs will be processed in a state estimation and transformation.

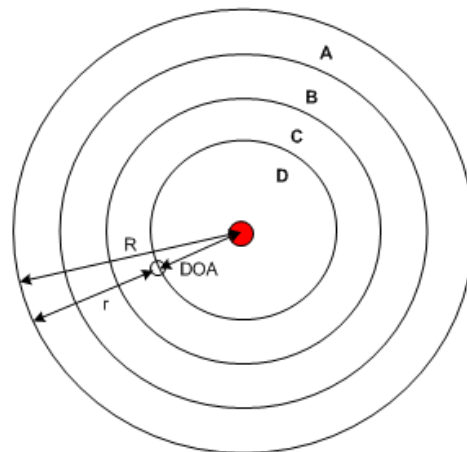


Figure 1. Security monitoring system space with the red circle denotes the valuable asset.

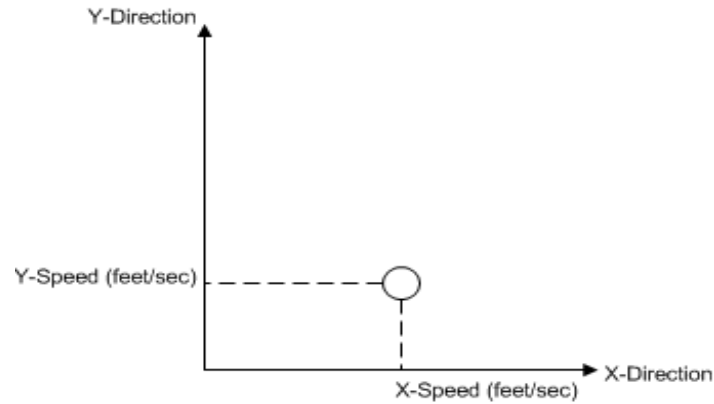


Figure 2. Agent speed captured on X and Y direction.

Finally sensor complementarity stage starts where sensor data fusion/complementarity is performed using type-2 fuzzy logic inference system to produce a suspiciousness decision for each moving agent as shown in Fig.3.

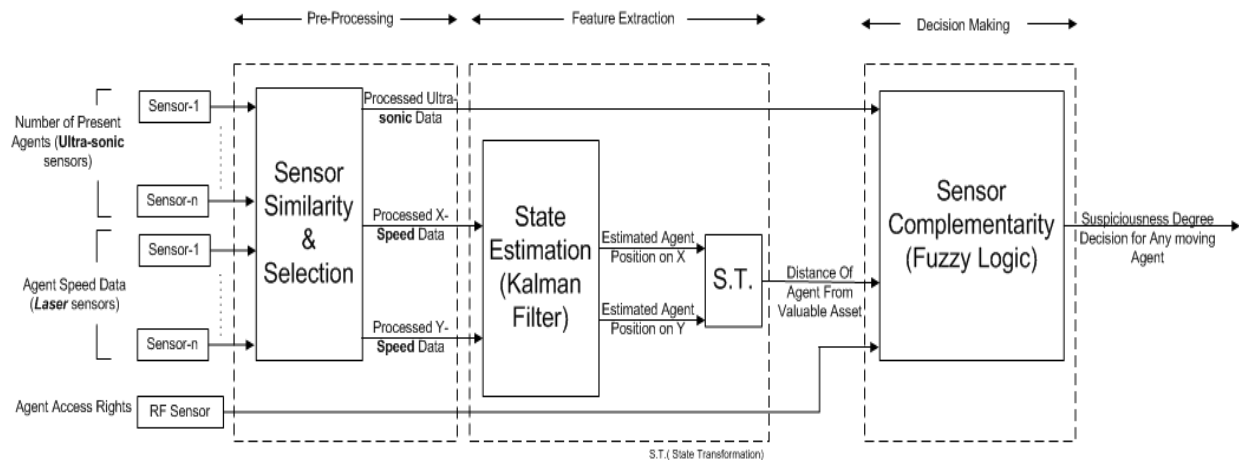


Figure 3. Security System Block Diagram.

IV. SENSOR SIMILARITY AND SELECTION

Considering raw sensor measurements directly into sensor fusion may affect quality of fusion which leads to making wrong decisions in some cases where these measurements contain noisy and inaccurate data. Thus, pre-processing of these sensors plays an important role in sensor fusion. Only reliable subsets of the sensors are needed; subsets that are consistent and accurate.

In our proposed system data is collected from a total of eight different laser sensors mounted on the X-axis and on the Y-axis (four sensors on each axis) with each sensor having different standard deviation and mean. This paper proposes a new method of sensor similarity that utilizes

the concepts of relative closeness of sensors with respect to each other. Over all mechanism of sensor similarity is summarized in Fig.4.

Sensors closeness in measurement between sensors is defined as the distance of sensor “j” with respect to other sensors on the same axis to be:

$$d_j = (Max(j)_{pos} - GA_{mean}) / \sigma_j^2 \quad (1)$$

where GA_{mean} is the Global Arithmetic mean of all sensors (on a given axis) and $Max(j)_{pos}$ is the best estimate of the true state of sensor “j” for data collected over one second time span sensor readings that are closest to the true state and defined as:

$$Max(j)_{pos} = Max[Posteriori(\hat{x}_j)] \quad (2)$$

where Posteriori of j^{th} sensor’s reading given the observation x_j is $P(s_j|x_j)$.



Figure 4. Flow chart shows how sensor similarity is performed.

a. Iterative Bayes estimate and Maximum Posteriori

In this estimate the posterior of the different sensors was obtained based on Bayes formula:

$$p(s|x) = \frac{p(x|s)p(s)}{p(x)} \quad (3)$$

Where “s” is the state and “x” is the observation. The probability of “s” given the observation “x”; the observation drawn from normal distribution $N(\mu, \sigma^2)$ where μ is the mean and standard deviation, so the mean of the likelihood function is the state under consideration which is represented as:

$$p(x|s) = \frac{1}{\sigma\sqrt{2\pi}} e^{\left(\frac{-(x-s)^2}{2\sigma^2}\right)} \quad (4)$$

and:

$$p(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{\left(\frac{-(x-\mu)^2}{2\sigma^2}\right)} \quad (5)$$

The only unknown term left in Bayes is $P(x)$. We know that:

$$\sum p(s|x) = 1 \quad (6)$$

so:

$$\sum \frac{p(x|s)p(s)}{p(x)} = 1 \quad (7)$$

then:

$$p(x) = \sum p(x|s)p(s) \quad (8)$$

The right side of equation (8) is computed for all observations and then divide by the total sum of these values to compute $P(x|s)$. This process was made iterative as more observations arrive by setting the priori $P_r(i+1) = \text{Posteriori}$ of the previous observation $P_o(i)$ and the maximum posteriori is pulled out at each iteration.

b. Global and Local Arithmetic Means

In this paper, the LA_{mean} is defined to be the Local Arithmetic Mean [12] for each sensor over its k observations and defined as:

$$LA_{mean} = (1/k) \sum_{i=1}^k x_i \quad (9)$$

and GA_{mean} in equation (1) to be the mean of all sensor local arithmetic means that is defined as follows:

$$GA_{mean} = \frac{\sum_{n=1}^4 LA_{mean}}{n} \quad (10)$$

where n : is the number of used sensors for an axis ($n = 4$ in our example) and finally, in equation (1) refers to the standard deviation of the sensor “ j ” given the fact that each sensor has a different mean and standard deviation.

After each sensor’s d_j is calculated it is compared to a pre-defined threshold distance d_{th} to determine if the reading of this sensor should be rejected or considered which constitutes the part of sensor selection. In this paper we assume threshold d_{th} is concluded from a previously conducted calibration of the sensor network.

If the sensor’s reading is considered then it is factored in when calculating the overall average of all considered readings:

$$Total_{average} = \frac{\sum_{i=1}^n LA_{mean_i}}{n} \quad (11)$$

where “ n ” here is the total number of accepted sensors.

Finally, a single reading as a similarity output is obtained. This algorithm of similarity is applied to laser sensors on both X axis and Y axis, and to the sonar sensors as well.

V. STATE ESTIMATION AND TRANSFORMATION

a. Kalman Filter

The method of Kalman filtering is a widely utilized for filtering sensor measurement data and for sensor data fusion as well [13].

Kalman filter uses measurements that are observed over time that contain noise, and produces values that tend to be closer to the true values of the measurements and their associated calculated values. The Kalman filter is a set of mathematical equations that provides an efficient computational (recursive) means to estimate the state of a process, in a way that minimizes the mean of the squared error. Kalman filtering is an ongoing cycle of time updating that projects the current state estimate ahead in time and the measurement updating that adjusts the projected

estimate by an actual measurement at that time. The equations for those two updates are presented below [14]:

The first step is the Prediction (Discrete KF time update):

(1) Project the state ahead:

$$\hat{x}_k = A_k \hat{x}_{k-1} + B_k u_k + w_k \quad (12)$$

Where x_k is the state vector (agent's position and velocity), A_k is the state transition model that is applied to the previous state x_{k-1} , B_k is the control input model that is applied to the control vector u_k and w_k is the process noise that is assumed to be drawn from a zero mean normal distribution with covariance Q .

$$p(w) \sim N(0, Q) \quad (13)$$

(2) Project the error covariance ahead:

$$P_k^- = A_k P_{k-1} A_k^T + Q \quad (14)$$

The second step is the Update (Discrete KF measurement update):

(1) Compute the KF gain:

$$K_k = P_k^- H^T (H P_k^- H^T + R)^{-1} \quad (15)$$

Where H is the measurement vector of the measurement z_k of the true state space:

$$z_k = H_k x_k + v_k \quad (16)$$

v_k is the measurement noise that is assumed to be drawn from a zero mean normal distribution with covariance R .

(2) Update estimate with measurement z_k :

$$\hat{x}_k = \hat{x}_k^- + K_k (z_k - H \hat{x}_k^-) \quad (17)$$

(3) Update the error covariance:

$$P_k = (1 - K_k H) P_k^- \quad (18)$$

For application purposes, estimates of the agent's position on the X and the Y axes of the space are needed. Kalman Filter was chosen to accomplish this task.

A system state was defined in this case to be the position and the speed.

$$V_x = X_Total_{average} \quad (19)$$

$$V_y = Y_Total_{average} \quad (20)$$

where the agent's speed at the X-axis is the final $X_Total_{average}$ that was arrived at. After collecting agent's data on X axis and deriving its corresponding position data as (same applies for the Y axis):

$$P_x = t * X_Total_{average} \quad (21)$$

$$P_y = t * Y_Total_{average} \quad (22)$$

Where, t is the time.

Kalman filter was applied on our system to estimate agent's next position.

b. State Transformation (Homogeneous Sensor Complementarity)

Multi-sensor complementarity is the synergistic use of the information provided by different sensory devices to assist in the accomplishment of a system task.

It refers to any stage in the integration process where there is an actual combination of different sources of sensory information into one sensory representation [15]. Sensor complementarities or correlation is especially advantageous when heterogeneous sensors are employed because of the potential to aggregate different views of the same incident.

For our application we are interested in the distance of an agent (DoA) from the valuable asset under surveillance; thus a transfer of the system state (agent's position on X and Y axes) to another form is needed where it describes the agent's distance with respect to asset. Since the agent could be moving in any direction in the space (its motion angle from asset will always change) we are always interested in that continuously changing distance. Therefore, we need to transform the X and Y to r and θ (Cartesian to polar). This is defined as homogeneous sensor complementarity as the system used reading from multiple sensors of the same type (speed on X and speed on Y). However, the system will only utilize the r (radial distance) part of that information then DoA is easily calculated to be $R-r$; where R is the radius of the largest circle where the agent is first detected by the sensors (Fig.1).

VI. DECISION MAKING/TYPE-2 FUZZY (HETREGONEOUS SENSOR COMPLIMENTARITY)

The last part of this proposed system is the security decision making which utilizes the previous sub-system output to make a decision using an interval type-2 fuzzy system since it is suitable to make a precise decision in uncertain circumstances.

a. Interval Type-2 Fuzzy Inference System

Unlike a type-1 set where the membership grade is a crisp value in [0, 1], a type-2 fuzzy set shown in Fig.5 is characterized by a fuzzy membership function, where the membership of each point of this set is a fuzzy set in [0, 1] [16].

An Interval type-2 fuzzy set makes room for non-deterministic truth degree and uncertainty [17, 18] (foot print of uncertainty FOU shown in Fig.5) for an element that belongs to a set. A type-2 fuzzy set denoted by, \tilde{A} , is characterized by a type-2 membership function, $\mu_{\tilde{A}}(x,u)$, where $x \in X$, $u \in J_x^u \subseteq [0,1]$ and $0 \leq \mu_{\tilde{A}}(x,u) \leq 1$.

$$(\tilde{A}) = \{(x, \mu_{\tilde{A}}(x)) \mid x \in X\} \tag{23}$$

$$(\tilde{A}) = \{(x, u, \mu_{\tilde{A}}(x, u)) \mid \forall x \in X, \forall u \in J_x^u \subseteq [0,1]\} \tag{24}$$

It is the bounded area in Fig.5 and mathematically it is the union of the upper and lower membership functions [15, 19], where the upper and lower memberships are Gaussian functions:

$$Upper(FOU(\tilde{A})) = N(m, \sigma_2; x) \tag{25}$$

$$Lower(FOU(\tilde{A})) = N(m, \sigma_1; x) \tag{26}$$

Where; σ_1 and σ_2 are the standard deviations for lower and upper membership functions respectively and m is the mean of both.

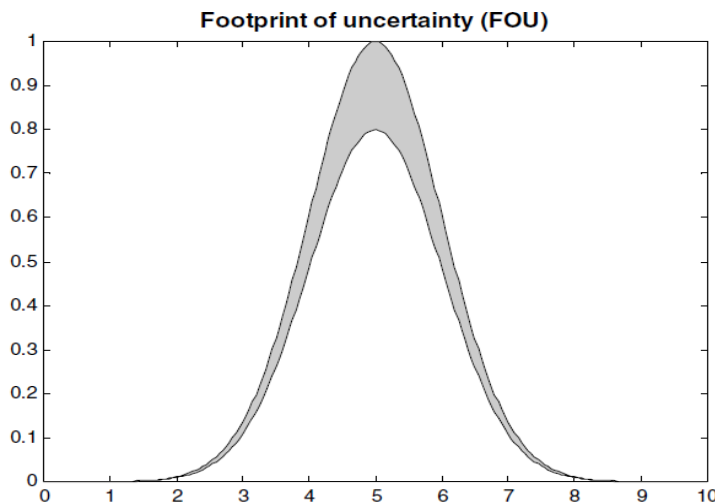


Figure 5. A Foot print of uncertainty of a sample interval type-2 Gaussian membership function.

b. Heterogeneous Sensor Complementarity

In this paper a decision making sub-system (an interval type-2 fuzzy logic system) is defined to be the heterogeneous sensor [19] complementarity as it reads in three different sensor data types and generates a fourth type of data that is totally different from the input ones. It is heterogeneous because it will generate a percentage output (percentage data type output) based on the number of agents (NoA that is different data type) and their relative distances from the valuable asset at any given time, the distance of agents (DoA that is a different data type) and finally, the agent's access rights (That is also different data type input).

The first input which is the "Number of Agents" (NoA) is considered an input with four different fuzzy ranges. Ranges are "Low" indicating the total number of objects is in the low scale of the alarming system, a "Medium Low" is the next level up, "Medium High" is the second highest level and finally "High" is the highest possible level. The second input is DoA_f that is generated as:

$$DoA_f = DoA * f \quad (27)$$

Where (DoA) "Distance of Agent" from the asset in feet. DoA is categorized into four different fuzzy categories, "Agent is extremely close", "Agent is very close", "Agent is close" and "Agent is far" (Fig.1). Also, where "f" is a multiplication factor that is based on the "Access Rights" of any moving agent and defined to be twenty for a "Trusted" (denoted by "T"), ten for "Semi-Trusted" (denoted by "ST") and finally a one for an "Unknown" agent (denoted by "U"). Fig. 6 shows the type-2 fuzzy logic membership functions for both Number of Agents and Distance of Agents.

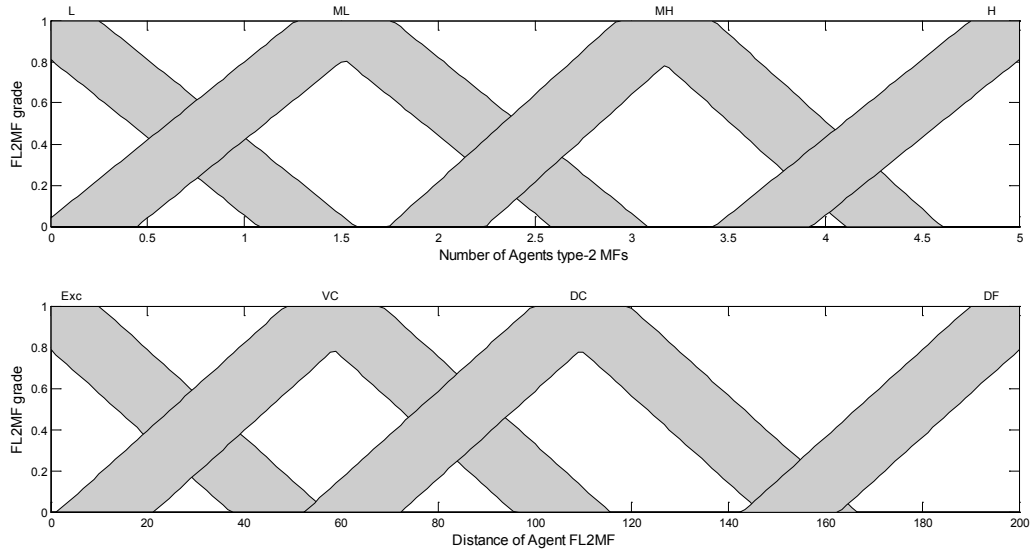


Figure 6. Interval type-2 Trapezoidal Membership functions for NoA and DoA respectively.

This was accomplished by setting a set of fuzzy inference system (FIS) rules (Fig. 7). Below is a sample of such rules:

If “Number of Agents” (NoA) is *High* and “Distance of Agent” (DoA) is *Extremely Close*

Then

“Degree of Suspiciousness” (DoS) is *Extremely Suspicious*

The proposed system has only one output which is the “Degree of suspiciousness” (DoS). This DoS is categorized into five levels of suspiciousness, “Not suspicious”, “Almost Suspicious”, “Suspicious”, “Very Suspicious”, and “Extremely suspicious” as shown in Fig.8 and is driven by the DoA_f and NoA inputs [6, 20].

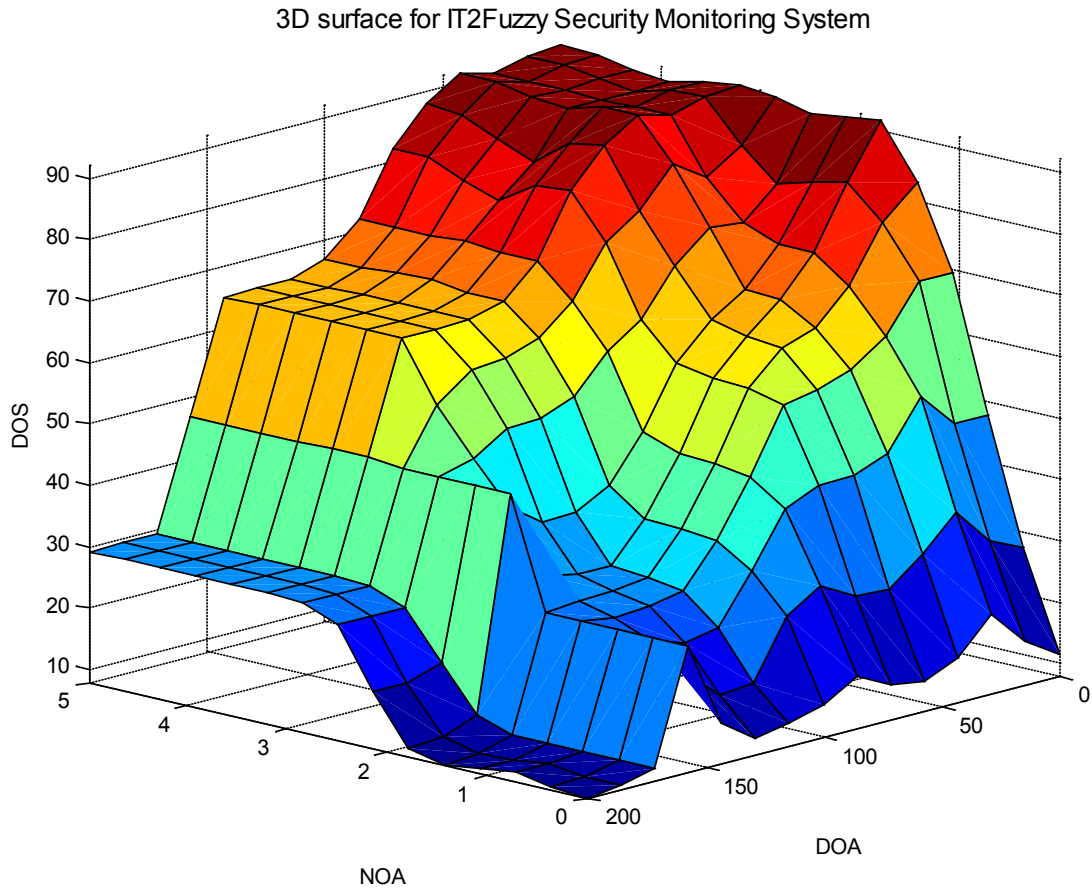


Figure 7. Interval type-2 Decision Surface Generated by FIS Rules.

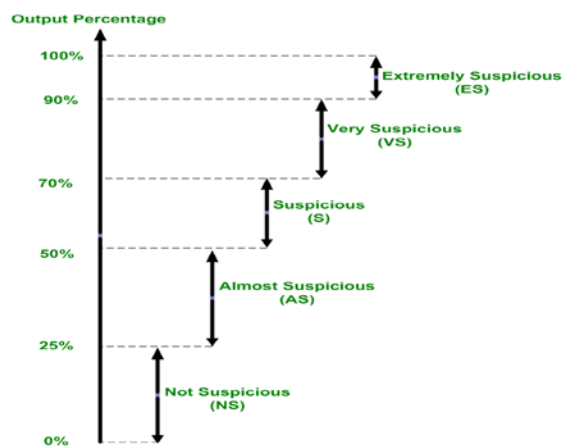


Figure 8. System Suspiciousness levels

VII. RESULTS AND DISCUSSION

In this paper a realistic simulation of several scenarios of agents moving linearly were investigated. Evaluation for a single agent is shown here. Assuming agent's true speed is 3 feet/sec on X-axis the grid of four sensors (each sensor is slightly different from the other in its mean and standard deviation) captured this speed over one second time frame. Fig.7 shows agent speed captured by four sensors.

Sensor 1 of this group is assumed to be noisier with mean and standard deviation well distant from the other three. It was also assumed the agent's true speed is 5 feet/sec on Y-axis, the grid of four sensors (each sensor is slightly different from the other in its mean and standard deviation) on this axis also captured this speed over same time interval that is 1 second Fig.8 shows this agent's data on the Y-axis. Sensor 2 of this group is assumed to be the noisy sensor.

Local Arithmetic means were next computed for each the four sensors on X-axis over for measurement over one second are shown in Fig.9 and Fig.10 shows their equivalents on the Y-axis for the same time span. The next step in our sensor similarity is to compute the maximum posteriori for each of the X-axis sensors which is displayed in Fig.11 and compute those posteriori for the Y-axis as well as shown in Fig.12. After sensor similarity is applied for both sets of laser sensors (X and Y axes), a distance for each sensor was calculated and compared to a pre-defined threshold values that are 0.5 and 0.9 for X and Y respectively.

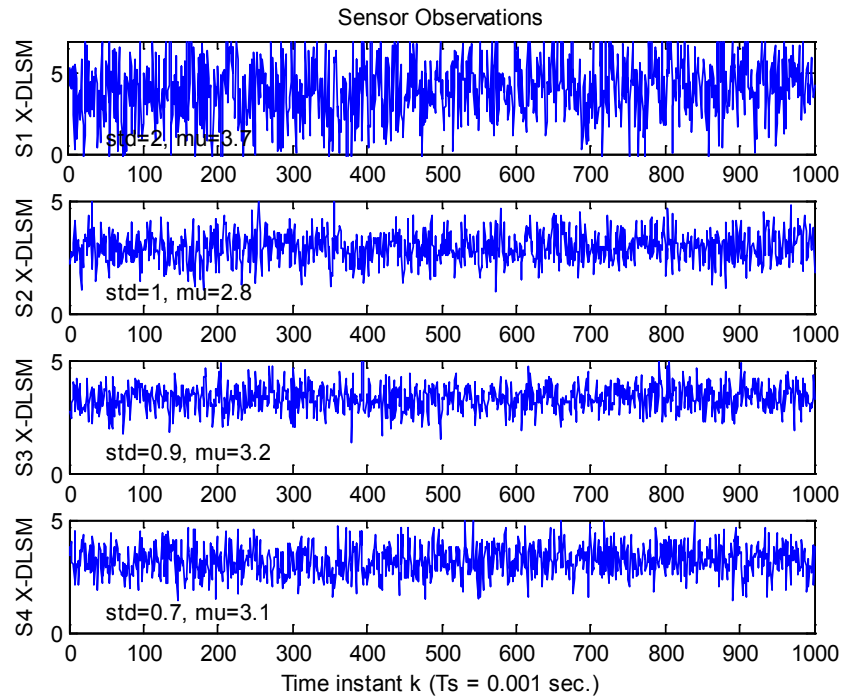


Figure 7. Speed data read by four Laser sensors on the X-axis of the sensor grid (where DLSM is Direction Laser Speed Measurement) and the number prefix refers to the sensor index in the grid.

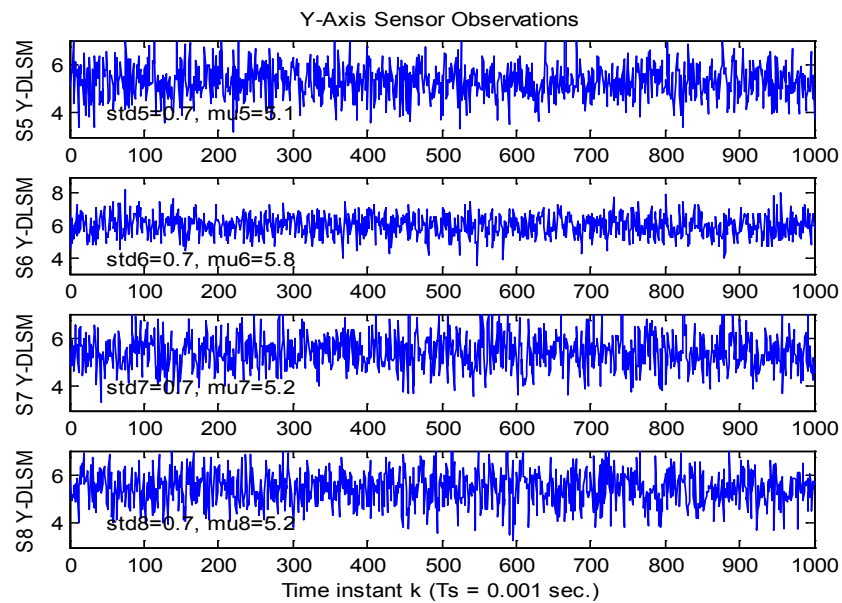


Figure 8. Speed data read by four Laser sensors on the X-axis of the sensor grid (where DLSM is Direction Laser Speed Measurement) and the number prefix refers to the sensor index in the grid

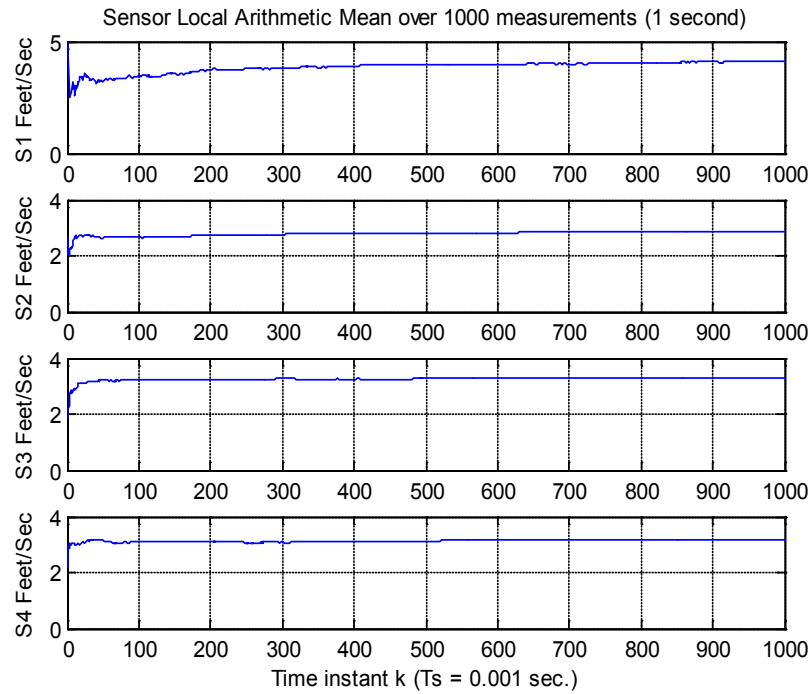


Figure 9. Local arithmetic mean (LAmean) for the four sensors on the X-axis over 1 second time span

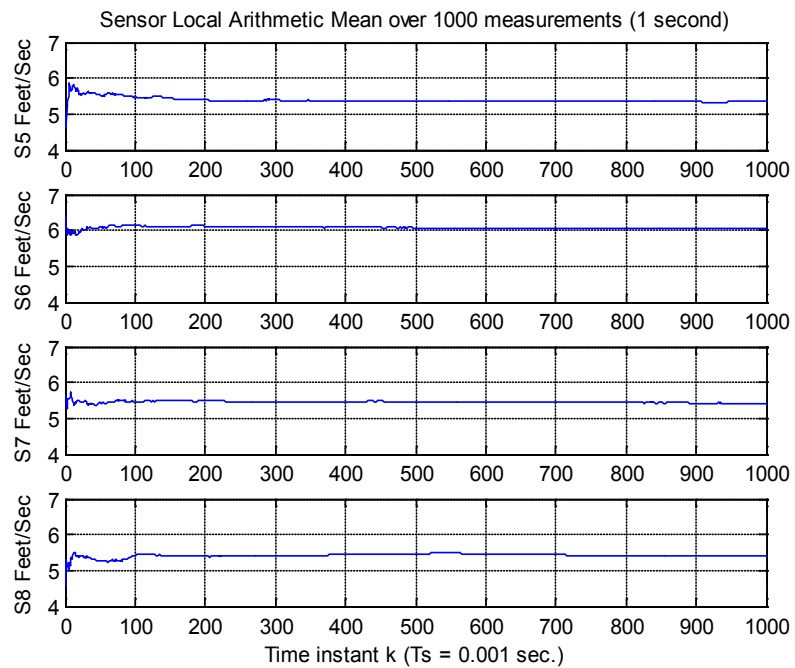


Figure 10. Local arithmetic mean (LAmean) for the four sensors on the Y-axis over 1 second time span

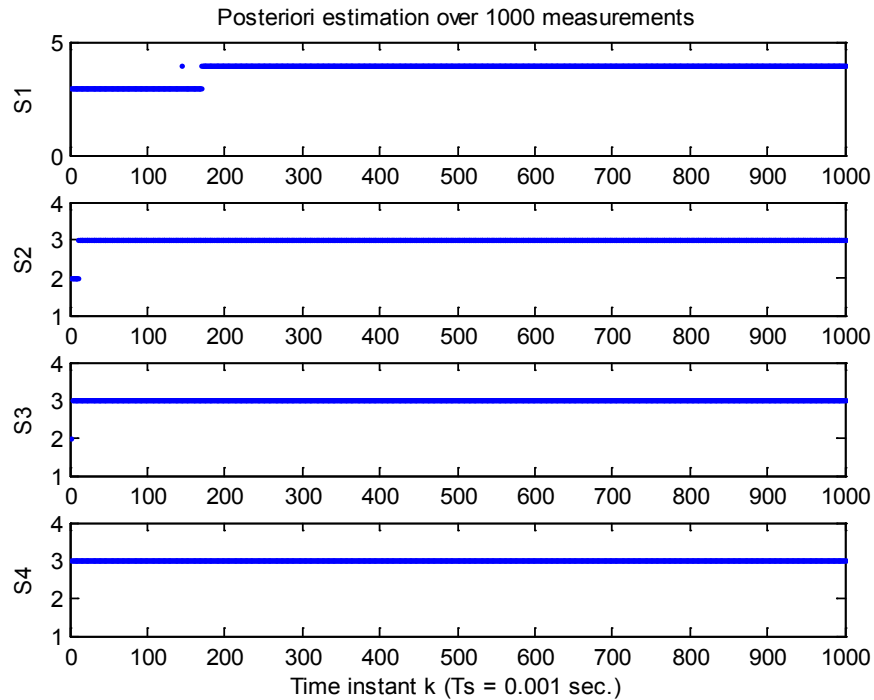


Figure 11. Max. Posteriori (Max(j)pos) for the four sensors on the X-axis over 1 second time span

Those thresholds are assumed to be based on sensor calibration data for each axis. New global arithmetic mean ($Total_{average}$) was computed but based on only accepted sensors. Next Kalman filter was used to estimate agent's next state (next accumulated distance) on both axes based on the $X_{Total_{average}}$ and $Y_{Total_{average}}$ that are shown in Fig.13 and Fig.14 respectively.

State estimation (S.T.) that is the second to last block in our security system is then utilized to transform the distance data on (x, y) coordinates to (r, θ) polar coordinates (homogeneous sensor complementarity) as in Fig.15.

Finally, a weighing is applied to this computed r (based on its access right that is chosen to be 1.3 and 1.1 for "Trusted" and "Semi-Trusted" respectively and 1 for "Unknown"). Then it is fed to the decision making system to decide on its suspiciousness degree at any time during its movement shown in Fig.16. This figure displays evaluation two agents having the same speed values but different access rights ("Trusted" and "Unknown").

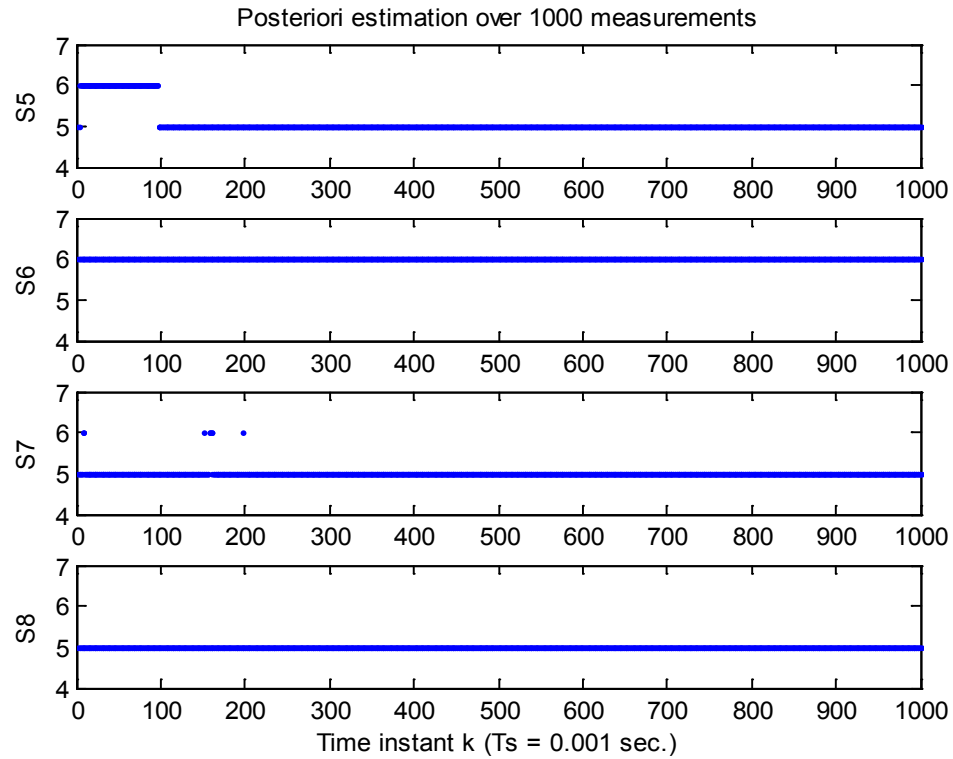


Figure 12. Max. Posteriori (Max(j)pos) for the four sensors on the Y-axis over 1 second time span

Fig.16 shows how the proposed security system was able to limit the DoS for the “Trusted” agent to less than 55%. However, it gave the “Unknown” agent almost a 65% for the same speed and distance accumulated values. It was shown that our system can actually use normal sensor data to filter it, estimate state, transform state and make a decision.

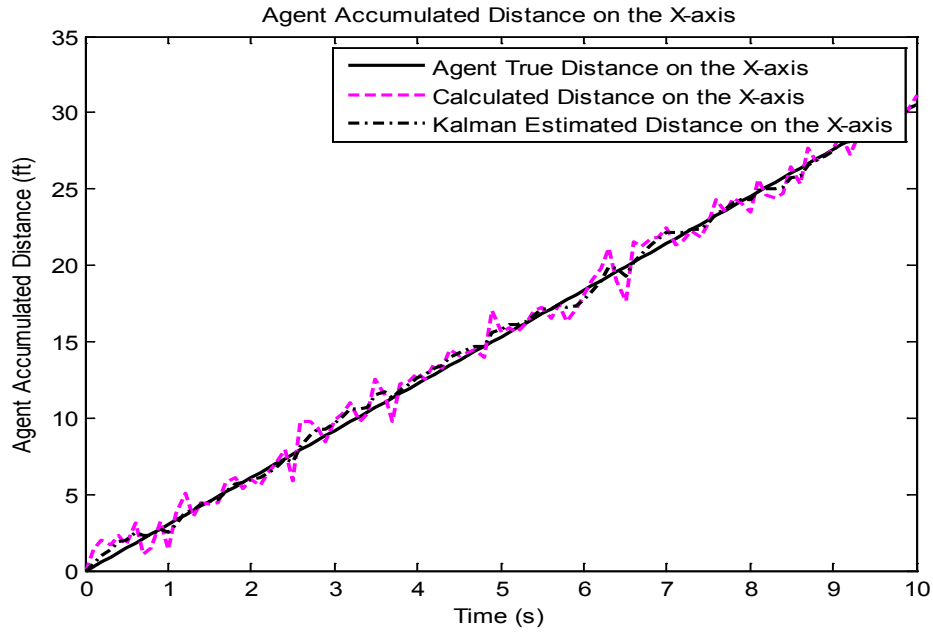


Figure 13. Agent position on X axis where “0” is the point where agent was first detected

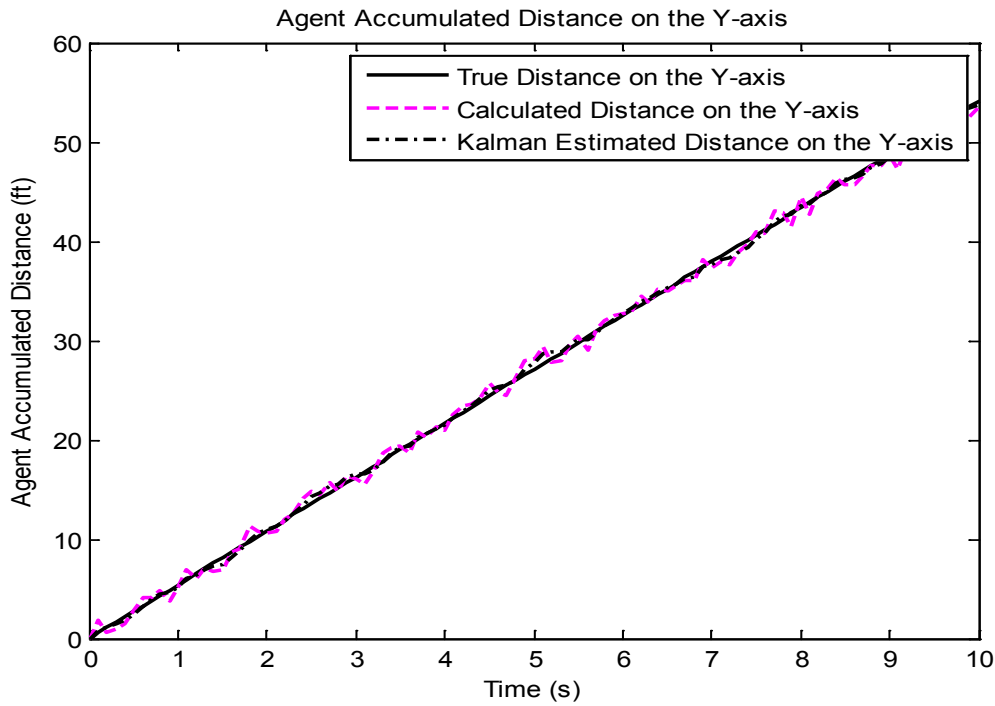


Figure 14. Agent position on Y axis where “0” is the point where agent was first detected

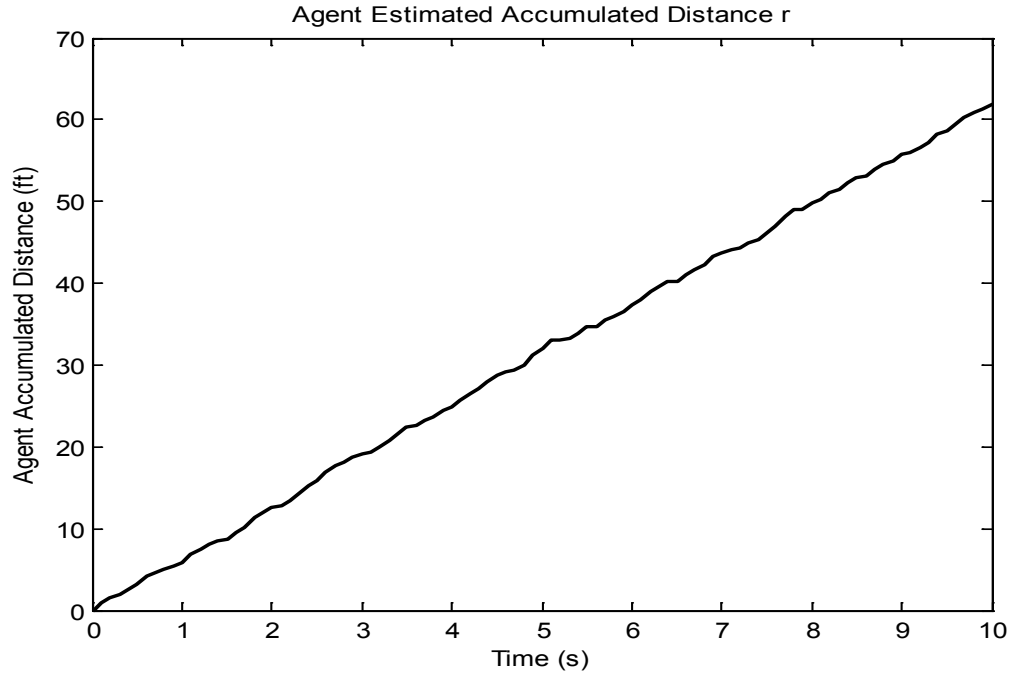


Figure 15. Agent accumulated distance in polar coordinates

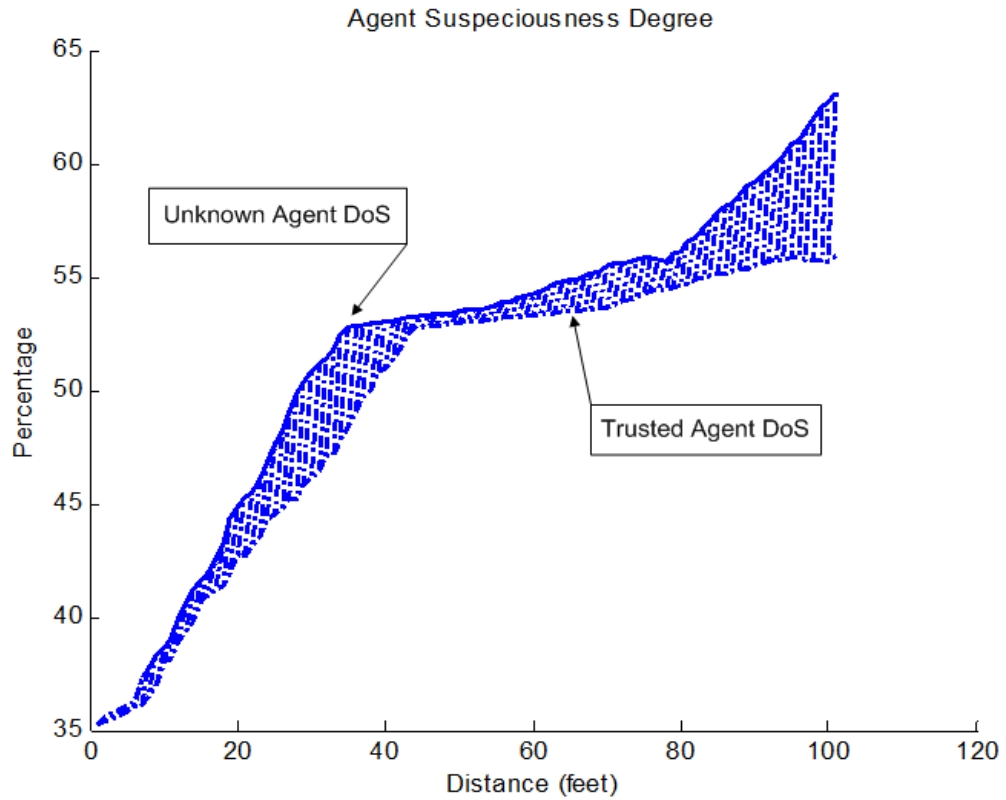


Figure 16. Agent suspiciousness degree as it moves

VIII. CONCLUSION AND FUTRUE WORK

Applying sensor similarity and complementarity (homogeneous and heterogeneous) concepts that are developed in this paper and helped improving the performance of a dynamic security monitoring system as they handled processing similar and different data types of multiple sensors. With Kalman filter and interval type-2 fuzzy inference help, the system was able to predict agent's next position and report its security status. The proposed system exhibits promising performance in security monitoring and agent security status evaluation.

One future system improvement is to introduce relationship between multiple agents.

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