



## A REVIEW OF ARTIFICIAL FISH SWARM OPTIMIZATION METHODS AND APPLICATIONS

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*Abstract- The Swarm Intelligence is a new and modern method employed in optimization problems. The Swarm Intelligence method is based on the en masse movement of living animals like birds, fishes, ants and other social animals. Migration, seeking for food and fighting with enemies are*

*social behaviors of animals. Optimization principle is seen in these animals. The Artificial Fish Swarm Optimization (AFSA) method is one of the Swarm Intelligence approaches that works based on the population and stochastic search. Fishes show very intelligently social behaviors. This algorithm is one of the best approaches of the Swarm Intelligence method with considerable advantages like high convergence speed, flexibility, error tolerance and high accuracy. this paper review the AFSA algorithm, its evolution stages from the start point up to now, improvements and applications in various fields like optimization, control, image processing, data mining, improving neural networks, networks, scheduling, and signal processing and so on. Also, various methods combining the AFSA with other optimization methods like PSO, Fuzzy Logic, Cellular Learning Automata or intelligent search methods like Tabu search, Simulated Annealing , Chaos Search and etc.*

**Index terms:** Artificial Fish Swarm Optimization, Swarm Optimization, Natural Computing.

## I. INTRODUCTION

Most species of animals show social behaviors. In some species this is the top member of the group which leads all members of that group. For example, this behavior is very apparent in lions, monkeys and deer. However, there are other kinds of animals which live in groups but have no leader. In this type of animals each member has a self organizer behavior which enables it to move around its environment and response to its natural needs with no need to leader like birds, fishes and sheep droves. This type of animals has no knowledge about their group and environment. Instead, they can move in the environment via exchanging data with their adjacent members. This simple interaction between particles makes group behavior more sophisticated as if we are looking for a particle in a wide environment.

This review considers Artificial Fish Swarm Optimization (AFSO), a relatively recent addition to the field of natural computing, that has elements inspired by the social behaviors of natural swarms, and connections with evolutionary computation. AFSO has found widespread application in complex optimization domains, and is currently a major research topic, offering an alternative to the more established evolutionary computation techniques that may be applied in many of the same domains.

This paper is structured as follows. Section 2 briefly reviews the general formulation of AFSO. Section 3 reviews the improved of AFSO .Section 4 reviews the motivations for, and research into, hybrid algorithms, many of which involve evolutionary techniques. Section 5

highlights some recent research into the application of AFSO to combinatorial problems. Section 6 concludes.

## II. GENERAL FORMULATION

In nature, the fish can find the more nutritious area by individual search or following after other fish, the area with much more fish is generally most nutritious. The basic idea of the AFSO is to imitate the fish behaviors such as praying, swarming, and following with local search of fish individual for reaching the global optimum [5]. The environment where an AF lives is mainly the solution space and is the states of other AFs. Its next behavior depends on its current state and its local environmental state (including the quality of the question solutions at present and the states of nearby companions). An AF would influence the environment via its own activities and its companions' activities.

A new evolutionary computation technique, Artificial Fish Swarm Optimization (AFSO) was first proposed in 2002 [1]. AFSO possess similar attractive features of genetic algorithm (GA) such as independence from gradient information of the objective function, the ability to solve complex nonlinear high dimensional problems. Furthermore, they can achieve faster convergence speed and require few parameters to be adjusted. Whereas the AFSO does not possess the crossover and mutation processes used in GA, so it could be performed more easily. AFSO is also an optimizer based on population. The system is initialized firstly in a set of randomly generated potential solutions, and then performs the search for the optimum one iteratively [6].

Artificial Fish (AF) is a fictitious entity of true fish, which is used to carry on the analysis and explanation of problem, and can be realized by using animal ecology concept. With the aid of the object-oriented analytical method, we can regard the artificial fish as an entity encapsulated with one's own data and a series of behaviors, which can accept amazing information of environment by sense organs, and do stimulant reaction by the control of tail and fin. The environment in which the artificial fish lives is mainly the solution space and the states of other artificial fish. Its next behavior depends on its current state and its environmental state (including the quality of the question solutions at present and the states of other companions), and it influences the environment via its own activities and other companions' activities [3].

The AF realizes external perception by its vision shown in Figure.1.  $X$  is the current state of a AF,  $Visual$  is the visual distance, and  $X_v$  is the visual position at some moment. If the state at the visual position is better than the current state, it goes forward a step in this direction, and arrives the  $X_{next}$  state; otherwise, continues an inspecting tour in the vision. The greater number of inspecting tour the AF does, the more knowledge about overall states of the vision the AF obtains. Certainly, it does not need to travel throughout complex or infinite states, which is helpful to find the global optimum by allowing certain local optimum with some uncertainty.

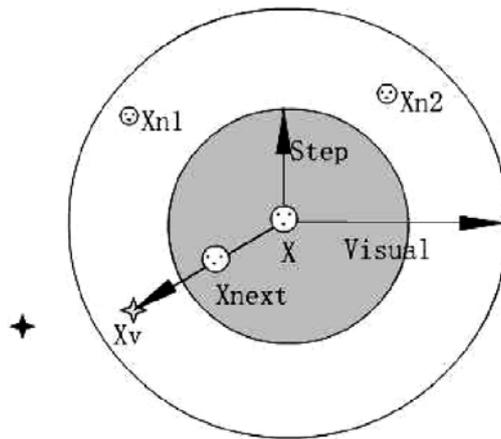


Figure. 1. Vision concept of the Artificial Fish

Let  $X = (x_1, x_2, \dots, x_n)$  and  $X_v = (x^v_1, x^v_2, \dots, x^v_n)$  then this process can be expressed as follows:

$$x_i^v = x_i + Visual.rand(), \quad i \in (0, n] \quad (1)$$

$$X_{next} = X + \frac{X_v - X}{\|X_v - X\|} \cdot Step.rand(). \quad (2)$$

Where  $Rand()$  produces random numbers between 0 and 1,  $Step$  is the step length, and  $x_i$  is the optimizing variable,  $n$  is the number of variables. The AF model includes two parts (variables and functions). The variables include:  $X$  is the current position of the AF,  $Step$  is the moving step length,  $Visual$  represents the visual distance,  $try\_number$  is the try number and  $\delta$  is the crowd factor ( $0 < \delta < 1$ ). The functions include the behaviors of the AF: AF\_Prey, AF\_Swarm, AF\_Follow, AF\_Move, AF\_Leap and AF\_Evaluate.

#### a. The Basic functions of AFSA

Fish usually stay in the place with a lot of food, so we simulate the behaviors of fish based on this characteristic to find the global optimum, which is the basic idea of the AFSA. The basic behaviors of AF are defined (9, 10) as follows for maximum:

**AF\_Prey:** This is a basic biological behavior that tends to the food; generally the fish perceives the concentration of food in water to determine the movement by vision or sense and then chooses the tendency. Behavior description: Let  $X_i$  be the AF current state and select a state  $X_j$  randomly in its visual distance,  $Y$  is the food concentration (objective function value), the greater *Visual* is, the more easily the AF finds the global extreme value and converges.

$$X_j = X_i + \text{Visual.rand}(\ ) \quad (3)$$

If  $Y_i < Y_j$  in the maximum problem, it goes forward a step in this direction;

$$X^{(t+1)}_i = X_i^{(t)} + \frac{X_j - X_i^{(t)}}{\|X_j - X_i^{(t)}\|} \cdot \text{Step.rand}(). \quad (4)$$

Otherwise, select a state  $X_j$  randomly again and judge whether it satisfies the forward condition. If it cannot satisfy after *try\_number* times, it moves a step randomly. When the *try\_number* is small in AF\_Prey, the AF can swim randomly, which makes it flee from the local extreme value field.

$$X_i^{(t+1)} = X_i^{(t)} + \text{Visual.rand}(\ ) \quad (5)$$

**AF\_Swarm:** The fish will assemble in groups naturally in the moving process, which is a kind of living habits in order to guarantee the existence of the colony and avoid dangers. Behavior description: Let  $X_i$  be the AF current state,  $X_c$  be the center position and  $n_f$  be the number of its companions in the current neighborhood ( $d_{ij} < \text{Visual}$ ),  $n$  is total fish number. If  $Y_c > Y_i$  and  $\frac{n_f}{n} < \delta$ , which means that the companion center has more food (higher fitness function value)

and is not very crowded, it goes forward a step to the companion center;

$$X^{(t+1)}_i = X_i^{(t)} + \frac{X_c - X_i^{(t)}}{\|X_c - X_i^{(t)}\|} \cdot \text{Step.rand}(). \quad (6)$$

Otherwise, executes the preying behavior. The crowd factor limits the scale of swarms, and more AF only cluster at the optimal area, which ensures that AF move to optimum in a wide field.

**AF\_Follow:** In the moving process of the fish swarm, when a single fish or several ones find food, the neighborhood partners will trail and reach the food quickly. Behavior description: Let  $X_i$  be the AF current state, and it explores the companion  $X_j$  in the neighborhood ( $d_{ij} < \text{Visual}$ ), which has the greatest  $Y_j$ . If  $Y_j > Y_i$  and  $\frac{n_f}{n} < \delta$ , which means that the companion

$X_j$  state has higher food concentration (higher fitness function value) and the surroundings is not very crowded, it goes forward a step to the companion  $X_j$ ,

$$X_i^{(t+1)} = X_i^{(t)} + \frac{X_j - X_i^{(t)}}{\|X_j - X_i^{(t)}\|} \cdot \text{Step.rand}(). \quad (7)$$

Otherwise, executes the preying behavior.

**AF\_Move:** Fish swim randomly in water; in fact, they are seeking food or companions in larger ranges.

**Behavior description:** Chooses a state at random in the vision, then it moves towards this state, in fact, it is a default behavior of AF\_Prey.

$$X_i^{(t+1)} = X_i^{(t)} + \text{Visual.rand}() \quad (8)$$

**AF\_Leap:** Fish stop somewhere in water, every AF's behavior result will gradually be the same, the difference of objective values (food concentration, FC) become smaller within some iterations, it might fall into local extremum change the parameters randomly to the still states for leaping out current state.

**Behavior description:** If the objective function is almost the same or difference of the objective functions is smaller than a proportion during the given  $(m-n)$  iterations, Chooses some fish randomly in the whole fish swarm, and set parameters randomly to the selected AF. The  $\beta$  is a parameter or a function that can make some fish have other abnormal actions (values),  $eps$  is a smaller constant.

$$\text{if } (BestFC(m) - BestFC(n)) < eps$$

$$X_{some}^{(t+1)} = X_{some}^{(t)} + \beta \cdot \text{Visual.rand}() \quad (9)$$

AF\_Swarm makes few fish confined in local extreme values move in the direction of a few fish tending to global extreme value, which results in AF fleeing from the local extreme values. AF\_Follow accelerates AF moving to better states, and at the same time, accelerates AF moving to the global extreme value field from the local extreme values.

### III. IMPROVED AFSA

ASFA is one of the best Swarm Intelligence algorithms. However, it has disadvantages including:

Higher time complexity, lower convergence speed, lack of balance between global search and local search, and not use of the experiences of group members for the next moves. It has many

advantages, such as good robustness, global search ability, tolerance of parameter setting, and it is also proved to be insensitive to initial values.

In recent years many researchers have attempted to improve this algorithm. In this section, a number of improvements are reviewed.

a. The Improved Basic Behaviors in AFSA1 [8]

To enhance the performance of the AFSA1[8], the information of global best AF is added to the behaviors of the AF. The realization of the behaviors in IAFSA is as follows for minimum:

a.i. Praying behavior (*AF\_Prey*):

Let  $X_i$  be the AF current state and select a state  $X_j$  randomly within visual distance,  $Y = f(\mathbf{X})$

is the food consistence of an AF:

$$X_j = X_i + af\_visual.rand() \quad (10)$$

If  $Y_i < Y_j$  in the minimum problem, it goes forward a step in the direction of the vector sum of the  $X_j$  and the  $X_{best\_af}$ ,  $X_{best\_af}$  is the best AF state in all AFs till now.

$$X_i^{t+1} = X_i^t + \left( \frac{X_j - X_j^t}{\|X_j - X_j^t\|} + \frac{X_{best\_af} - X_i^t}{\|X_{best\_af} - X_i^t\|} \right) * af\_step * rand() \quad (11)$$

Otherwise, select a state  $X_j$  randomly again and judge whether it satisfies the forward requirement. If the forward requirement cannot be satisfied after *try\_number* times, the AF would move a step randomly; this can help the AF flee from the local extreme field.

$$X_i^{t+1} = X_i^t + af\_visual * rand() \quad (12)$$

a.ii. Swarming behavior (*AF\_Swarm*):

Let  $X_i$  be the AF current state,  $X_c$  be the center position of several AF and  $n_f$  be the number of its companions within the AF's visual range. If  $Y_c < Y_i$  and  $Y_c < af\_delta * Y_i / n_f$ , which means that the fellow center has lower fitness value and the surrounding environment is not very crowded, and then the AF goes forward a step in the direction of the vector sum of the  $X_c$  and the  $X_{best\_af}$ .

$$X_i^{t+1} = X_i^t + \left( \frac{X_c - X_i^t}{\|X_c - X_i^t\|} + \frac{X_{best\_af} - X_i^t}{\|X_{best\_af} - X_i^t\|} \right) * af\_step * rand() \quad (13)$$

Otherwise, the preying behavior is executed.

a.iii. Following behavior (*AF\_Follow*):

Let  $X_i$  denote the AF current state, and the AF explores its neighborhood area to find the AF  $X_j$  which has the smaller  $Y_j$ . If  $Y_j < Y_i$  and  $Y_j < af\_delta * Y_i / n_f$ , which means that the AF  $X_j$  has lower fitness value and the surrounding environment is not very crowded, the AF  $X_i$  goes forward a step in the direction of the vector sum of the  $X_j$  and the  $X_{best\_af}$ .

$$X_i^{t+1} = X_i^t + \left( \frac{X_j - X_i^t}{\|X_j - X_i^t\|} + \frac{X_{best\_af} - X_i^t}{\|X_{best\_af} - X_i^t\|} \right) * af\_step * rand() \quad (14)$$

a.iv. Moving behavior (*AF\_Move*):

The AF chooses a state randomly within the visual range, and then it moves towards this state, it is a default behavior of an AF.

$$X_i^{t+1} = X_i^t + af\_visual * rand() \quad (15)$$

a.v. Other behaviors

Other behaviors of IAFSO1 such as leaping behavior and evaluating behavior are the same as AFSO. The leaping behavior [3] is proposed to increase the probability to leap out local extremes. The evaluating behavior is based on the evaluation to the environment of an AF, and can help the AF select a proper behavior to execute. The swallowing behavior [8] is executed if the fitness function value is bigger (for minimum optimization) than a given threshold in updating process of AFSO.

Experimental results show that the IAFSO1 has advantages of *faster convergence speed* and *higher global search accuracy* than the standard AFSO by adding limited computing complexity, because of its good performance, the IAFSO1 might replace the AFSO in future optimization applications.

b. cultured Artificial Fish-swarm Algorithm (CAFAC) [9]

A novel cultured AFSA (Artificial Fish-swarm Algorithm) with the crossover operator, namely CAFAC [9], is proposed to enhance its optimization performance. The crossover operator utilized is to promote the diversification of the artificial fish and make them inherit their parents' characteristics. The Culture Algorithms (CA) is also combined with the AFA so that the blind search can be combated with.

In the CAFAC, a crossover operator is utilized to improve the diversification of the artificial fish and make the artificial fish inherit their parents' characteristics. The CA is further combined with the modified AFA together to overcome the shortcoming of blind search. A total of 10 high-dimension and multi-peak functions are employed to examine the

performance of our CAFAC. Simulation results show that it can indeed outperform the original AFA.

#### c. Improved Artificial Fish-swarm optimization (IAFSO2) [10]

In order to improve the algorithm's stability and the ability to search the global optimum, they propose an improved AFSO (IAFSO)[10]. When the artificial fish swarm's optimum value is not variant after defined generations, they add leaping behavior and change the artificial fish parameter randomly. By the way, they can increase the probability to obtain the global optimum.

##### c.i. The elimination of step restriction

In the AFSO, the step of artificial fish is a random number in  $(0, \text{step})$  while they execute searching behavior, swarming behavior and chasing behavior. The three AF's behaviors are local actions which increase the probabilities of individual evolution and premature. The actual step of IAFSO2 is a random number in the defined area to guarantee the better global search capacity.

##### c.ii. The leaping behavior

The searching behavior, swarming behavior and chasing behavior are all local behaviors in some degree. If the objective functions value is not changed after several iterations, it manifests that the function might fall into local minimum. If the program continues iterating, every AF's result will gradually be same and the probability of leaping out local optimum will be smaller. To increase the probability to leap out local optimum and attain global optimum, they attempt to add leaping behavior to AF.

The AF's leaping behavior is defined as follow. If the objective value's difference between  $K$  times and  $K+N$  times is smaller than  $eps$  in the iteration process, we select randomly an AF according to the proportion  $p(0 < p < 1)$  and change its parameters randomly in the defined area.

AFSO is a novel method to search global optimal value by AF's searching behavior, swarming behavior and chasing behavior. The step constrains in the three behaviors affects the global search capacity of the AF. Therefore, they eliminate the step constrain in IAFSO2. In addition, they add leaping behavior to AFSO in order to reduce the possibility of AF falling into local optimum. They design the data structure and procedure in order to apply AFSO and IAFSO2 to the training process of three layouts feed-forward neural networks and the comparison result demonstrates that the IAFSO2 has better global astringency and stability.

Therefore, the improvement of AFSO in the paper is effective, and IAFSO2 is an effective method to train feed-forward neural networks.

#### d. Improved Artificial Fish-swarm optimization (IAFSO3) [11]

The algorithm herein presented is a modified version of the artificial fish swarm algorithm for global optimization [11]. The new ideas are focused on a set of movements, closely related to the random, the searching and the leaping fish behaviors. An extension to bound constrained problems is also presented. To assess the performance of the new fish swarm intelligent algorithm, a set of seven benchmark problems is used. A sensitivity analysis concerning some of the user defined parameters is presented.

They present a new version of the artificial fish swarm algorithm, herein denoted by Fish Swarm Intelligent (FSI) algorithm. Our modifications are focused on:

1. The extension to bound constrained problems meaning that any fish movement will be maintained inside the bounds along the iterative process;
2. Modified procedures to translate random, searching and leaping fish behaviors;
3. The introduction of a selective procedure;
4. Different termination conditions.

The four main algorithms are shown in the following:

```

Algorithm 2 Random
input:  $x^i, l, u, \text{"visual"}$ 
for  $k = 1, \dots, n$  do
     $\lambda_1 \sim U[0, 1]; \lambda_2 \sim U[0, 1]$ 
    if  $\lambda_1 > 0.5$  then
        if  $u_k - x_k^i > \text{"visual"}$  then
             $y_k = x_k^i + \lambda_2 \text{"visual"}$ 
        else
             $y_k = x_k^i + \lambda_2(u_k - x_k^i)$ 
        end if
    else
        if  $x_k^i - l_k > \text{"visual"}$  then
             $y_k = x_k^i - \lambda_2 \text{"visual"}$ 
        else
             $y_k = x_k^i - \lambda_2(x_k^i - l_k)$ 
        end if
    end if
end for
    
```

```

Algorithm 1 fish swarm intelligent algorithm
Input:  $m, l, u, nfe_{max}, \varepsilon, \delta, \mu\delta, \theta, \eta$ 
iteration  $\leftarrow 1; \tau \leftarrow 1$ 
 $(x^1, \dots, x^m) \leftarrow Initialize()$ 
while termination criteria are not satisfied do
    for  $i = 1, \dots, m$  do
        Compute the "visual"
        if visual scope is empty then
             $y^i \leftarrow Random(x^i)$ 
        else
            if visual scope is crowded then
                 $y^i \leftarrow Search(x^i)$ 
            else
                if central point is better than  $x^i$  then
                     $y_1^i \leftarrow Swarm(x^i)$ 
                else
                     $y_1^i \leftarrow Search(x^i)$ 
                end if
                if best function value is better than  $f(x^i)$  then
                     $y_2^i \leftarrow Chase(x^i)$ 
                else
                     $y_2^i \leftarrow Search(x^i)$ 
                end if
                 $y^i \leftarrow \arg \min\{f(y_1^i), f(y_2^i)\}$ 
            end if
        end if
    end for
    for  $i = 1, \dots, m$  do
         $x^i \leftarrow Select(x^i, y^i)$ 
    end for
    if iteration  $> \tau m$  then
        if "stagnation" occurs then
            Randomly choose a point  $x^l$ 
             $y^l \leftarrow Leap(x^l)$ 
        end if
    end if
     $\tau \leftarrow \tau + 1$ 
end while
    
```

```

Algorithm 3 (Movement along a particular direction)
input:  $x^i, l, u, d^i$ 
 $\lambda \sim U[0, 1]$ 
for  $k = 1, \dots, n$  do
    if  $d_k^i > 0$  then
         $y_k^i \leftarrow x_k^i + \lambda \frac{d_k^i}{|x_k^i|} (u_k - x_k^i)$ 
    else
         $y_k^i \leftarrow x_k^i - \lambda \frac{d_k^i}{|x_k^i|} (x_k^i - l_k)$ 
    end if
end for
    
```

```

Algorithm 4 (Leaping behavior)
input:  $x, l, u$ 
rand  $\sim U\{1, \dots, m\}$ 
for  $k = 1, \dots, n$  do
     $\lambda_1 \sim U[0, 1]; \lambda_2 \sim U[0, 1]$ 
    if  $\lambda_1 > 0.5$  then
         $y_k^i \leftarrow x_k^i + \lambda_2(u_k - x_k^i)$ 
    else
         $y_k^i \leftarrow x_k^i - \lambda_2(x_k^i - l_k)$ 
    end if
end for
    
```

#### IV. HYBRID AFSA

Despite of its many advantages, the AFSA has some disadvantages. Different researchers have tried to improve this algorithm by using different algorithm and combining them with this algorithm. In this paper, some of these composite approaches are reviewed.

##### a. CF-AFSA

A Hybrid Artificial Fish Swarm Algorithm, which is combined with CF and Artificial Fish Swarm Algorithm, is proposed in this paper to solve the Bin packing problem. Experiment results compared with GA shows that the Hybrid Artificial Fish Swarm Algorithm has a good performance with broad and prosperous application [12].

The dimension of search space is established as  $n$ , the scale of fish  $N$ . Each artificial fish can be expressed as a vector of  $n$  dimension  $X_i = (x_{i1}, x_{i2}, \dots, x_{in})$  ( $i = 1, 2, \dots, N$ ); function  $Y=f(X)$  shows the current concentration of food of artificial fish;  $d_{i,j} = d(X_i, X_j)$  ( $i, j = 1, 2, \dots, N$ ) means the distance between the artificial fish  $X_i$  and the artificial fish  $X_j$ ;  $\delta$  signifies congestion degree factor; *TryNumber* indicates the largest trying number of each movement of artificial fish; *Visual* means the field of vision of artificial fish.

##### a.i THE DESCRIPTION OF ALGORITHM

Step 1: Initialization

Step2: Calculate fitness value

Step3: Each artificial fish  $i$  ( $i = 1, 2, \dots, N$ )

Step3.1: Following; judge whether the state after following is better than the previous state, and if so, turn to.

Step4, otherwise turn to Step3.2;

Step3.2: Clustering; judge whether the state after clustering is better than the previous state, and if so, turn to.

Step4, otherwise turn to Step3.3;

Step3.3: Foraging;

Step4: Update the current best value;

Step5: Update the distance among fish swarm  $d_{i,j}, (i, j = 1, 2, \dots, N)$

Step6: If already achieve the maximum evolution algebra, exit; otherwise, turn to Step3.

b. AFSA-PSO (HAP)

A hybrid of artificial fish swarm algorithm (AFSA) and particle swarm optimization (PSO) is used to training feed forward neural network. After the two algorithms are introduced respectively, the hybrid algorithm based on the two is expressed. The hybrid not only has the artificial fish behaviors of swarm and follow, but also takes advantage of the information of the particle. An experiment with a function approximation is simulated, which proves that the hybrid is more effective than AFSA and PSO [13].

b.i. Behavior of searching food

In general, the fish stroll at random. When the fish discover a water area with more food, they will go quickly toward the area. Let us assume that  $X_i$  is the AF state at present, and  $X_j \in S$ .

The behavior of follow can be expressed as the following:

$$prey(X_i) = \begin{cases} X_i + step \frac{X_j - X_i}{\|X_j - X_i\|} & \text{if } y_j > y_i \\ X_i + step & \text{else} \end{cases} \quad (16)$$

b.ii. Behavior of swarm

In the process of swimming, the fish will swarm spontaneously in order to share the food of the swarm. Let us assume that  $X_i$  is the AF state at present, and  $X_c = \sum_{x \in S} X_j / nf$ . The behavior of swarm to AF  $i$  can be expressed in Formula 4.

$$swarm(X_i) = \begin{cases} X_i + step \frac{X_c - X_i}{\|X_c - X_i\|} & \text{if } \frac{y_c}{nf} > \delta y_i \\ prey(X_i) & \text{else} \end{cases} \quad (17)$$

b.iii. Behaviors of Agents

When one fish of the fish swarm discovers more food, the other fish will share with it. Let us assume that  $X_i$  is the AF state at present, and  $y_{\max} = \max\{f(X_j) | X_j \in S\}$ . The behavior of follow can be expressed in Formula 5.

$$follow(X_i) = \begin{cases} X_i + step \frac{X_{\max} - X_i}{\|X_{\max} - X_i\|} & \text{if } \frac{y_{\max}}{nf} > \delta y_i \\ prey(X_i) & \text{else} \end{cases} \quad (18)$$

According to the character of the problem, the AF evaluates the environment at present, and then selects an appropriate behavior. For example, behaviors of follow and swarm are both simulated, the better of improved its state will be executes. This process indicates the flexibility of AFSA.

MFNN training by a new algorithm, HAP, is proposed. HAP is a hybrid of PSO and AFSA; it has the advantages of the two at the same time. When the information of the AFSA is enough, AFSA will be executed, and otherwise, the PSO will be executed. With the above performance, HAP is a good algorithm to training MFNN. To demonstrate the performance of HAP, designs of function approximation with three layers ANN are simulated.

#### c. AFSA- SFLA

In order to overcome the defects of Shuffled Frog Leaping Algorithm (SFLA) such as slow searching speed in the late evolution and easily trapping into local extremum, a Composite Shuffled Frog Leaping Algorithm (CSFLA) based on the basic idea of Artificial Fish-Swarm Algorithm (AFSA) is put forward in this paper in which the follow behavior of fish swarm is used to accelerate the optimization speed and the swarm behavior to improve the capacity of out of local extremum. The test results indicate that CSFLA increases the convergence velocity outstandingly and enhances the global searching performance effectively [14].

#### d. AFSA – CLA

A new algorithm which is obtained by hybridizing cellular learning automata and artificial fish swarm algorithm (AFSA) is proposed for optimization in continuous and static environments. In the proposed algorithm, each dimension of search space is assigned to one cell of cellular learning automata and in each cell a swarm of artificial fishes are located which have the optimization duty of that specific dimension. In fact, in the proposed algorithm for optimizing D-dimensional space, there are D one-dimensional swarms of artificial fishes that each swarm is located in one cell and they contribute with each other to optimize the D-dimensional search space. The learning automata in each cell are responsible for making diversity in artificial fishes swarm of that dimension and equivalence between global search and local search processes. The proposed algorithm with standard AFSA, Cooperative Particle swarm optimization (PSO) and global version of PSO in 10 and 30-dimensional spaces are practiced on six standard fitness functions. Experimental results show that presented method has an acceptable performance [15].

#### e. CSA- AFSA

This hybrid method, a QoS multicast routing algorithm based on clonal selection and artificial fish swarm algorithms (CSA-AFSA). The hybrid algorithms reasonably use the superiorities

of both algorithms and try to overcome their inherent drawback. An improved initialization method is used to make sure each individual in initial population is a reasonable multicast tree without loops. The simulation carried out with different network scale. The results have demonstrated the hybrid algorithm has high speed of convergence and searching capability to solve QoS multicast routing effectively [16].

#### f. CAFSA

According to the characteristics of Artificial Fish-swarm Algorithm and Chaos Optimization Algorithm, A

kind of artificial Fish-Swarm Algorithm with Chaos is constructed by adding chaos to influence the update of the velocities of artificial fish, so that precocious phenomenon is suppressed, the convergence rate and the accuracy is improved. By testing two functions and NP hard problems of the Planar Location Problem, the experimental results show that the algorithm is an efficient global optimization algorithm for solving global optimization problem [22].

In view of the defects of AFSA with slow convergence in the later period, low optimizing precision, and on some issues fall into local optimum easily. As well as the characteristics of chaos with ergodicity and sensitivity to the initial value, add chaos to AFSA, guide the current optimized individual fish with Chaos iteration to further optimization. The main steps of Artificial Fish-Swarm Algorithm with Chaos are as follows:

Step1: Parameter setting, initialize the state of fish (population size is  $N$ ). In the feasible region generate  $N$  artificial fish individual randomly,  $visual$  is the greatest perception distance of artificial fish,  $Step$  is the largest step,  $\delta$  is crowd factor,  $n$  is the largest number of each artificial fish try to search food,  $c$ ,  $d$  are chaotic mutation parameters.

Step2: Initialization of bulletin board. Calculate the function value of each initial fish and compare the value, assign the best artificial fish to its bulletin board.

Step3: Selecting behavior. Each artificial fish simulate the swarming and following behavior respectively, and select the best behavior to perform by comparing the function values, the default is searching food behavior.

Step4: Chaotic mutation. Perform mutation to the current status of each fish depend on  $X_{i,next} = X_i + c \cdot t_i - d$ , if the status out of the feasible region, then generate  $X_{i,next}$  in feasible region randomly. Calculate  $f(X_{i,next})$ , if  $f(X_{i,next})$  is superior to  $f(X_i)$ , then,  $X_i = X_{i,next}$  Otherwise, do not update; set  $t_i = 4t_i(1-t_i)$ .

Step5: Update bulletin board. According to the latest status of each fish, update bulletin board by comparing its fitness value, optimal state is  $X_{best}$ .

Step6: Perform chaotic mutation to the current optimal state of fish that on the Bulletin board. Perform chaotic mutation to the optimal state depend on  $X_{next} = X_i + cu - d$ , if the status out of the feasible region, do not update. Calculated function values  $f(X_{cbest})$ , if  $f(X_{cbest})$  superior to  $f(X_{best})$ , then,  $X_{best} = f(X_{cbest})$  otherwise, do not update; set  $u = 4u(1-u)$ .

Step7: Check the termination condition. If meet, then jump out of iterative and output the optimal value; otherwise, turn to step3.

Testing it with six-hump camel back function and Applying it to PLP demonstrates that the results that this hybrid algorithm has got better than AA has got. This algorithm can solve the constrained and unconstrained problem effectively.

#### g. CSAFSA

The idea of CSAFSA brings the CS mechanism into the operation flow of AFSA. On one hand it can enhance the global search capabilities and get out of the local optimum easily. While on the other hand, it will not reduce the convergence speed and search accuracy at the same time. When all of the AF has completed one movement, evaluate the global best fish, and then use the chaos optimization algorithm to search around the position of best fish within a certain radius. If better, then replace the global best fish with this solution [17]. The execution of CSAFSA is as follows:

Step 1: Generate the initial fish swarm randomly in the search space;

Step 2: Initialize the value of bulletin board, calculate the current function value  $y$  of each AF, and assign the value of best fish to bulletin board;

Step 3: Simulate fish following behavior and fish swarming behavior respectively, and then select the behavior Results in better function value  $y$ , and the default behavior is fish preying;

Step 4: Check the function value  $y$  with the value of bulletin board. If better, then replace it;

Step 5: Perform chaos search near the current best AF. If better solution has been found, then replace the global best fish with this solution;

Step 6: Judge whether the preset maximum iteration number has achieved or a satisfactory optimum solution has obtained. If not satisfied, go to step 3. Otherwise go to step 7;

Step 7: Output the optimum solution.

#### h. ICAFSA

As a newly-proposed stochastic global optimization algorithm, artificial fish swarm algorithm (AFSA) is featured by its good global convergence and high convergence speed. However, it may suffer from the problem of being trapped in local optimum and it has relatively low search accuracy. Having analyzed the deficiencies of AFSA and making use of the ergodicity and internal randomness of chaos optimization algorithm (COA), this research further puts forward an improved chaotic artificial fish swarm algorithm (ICAFSA). In this improved algorithm, chaos optimization is first employed to initialize the position of individual artificial fish and then AFSA is applied to obtain the neighborhood of the global optimum solution. When there is no change or little change of the function values on bulletin board in successive iterations, chaotic mutation is then executed to help the artificial fish swarm get rid of the local optimum. The findings of case study show the feasibility and effectiveness of the ICAFSA in the optimization operations of cascade hydropower stations [19].

Improved chaotic artificial fish swarm algorithm (ICAFSA) has coupled the characteristics of chaos search into the searching process of AFSA, in order to make up for the deficiency of being easily trapped into the local optimum of AFSA in the latter phase. The process of chaos mutation is as follows [20]:

(1) Let the  $k$  th generation of AF be  $Z^k = (Z_1^k, Z_2^k, \dots, Z_n^k)$  then map the variables to chaotic variable interval (0,1) respectively to form chaotic variable sequence  $Z^{k*}$ ,

$Z^{k*} = (Z_1^{k*}, Z_2^{k*}, \dots, Z_n^{k*})$  the mapping equation is as follows:

$$Z_i^{k*} = \frac{Z_i^k - a_i}{b_i - a_i} \quad (19)$$

Among which,  $a_i$  and  $b_i$  are the minimum and maximum of the  $i$  th variable of  $Z^k$  respectively.

(2) The chaotic variable  $Y = (Y_1, Y_2, \dots, Y_n)$  produced by Logistic Mapping Method is added to the variable  $Z^{k*}$  by certain probability, and then map the chaotic mutation individuals to interval (0, 1) as follows:

$$W_i^{k*} = Z_i^{k*} + \alpha \cdot Y_i \quad (20)$$

Among which,  $Z^{k*}$  and  $W_i^{k*}$  are the chaotic values of the  $i$  th variable of  $Z^{k*}$  and  $W_i^{k*}, Y_i$  is the value of the  $i$  th variable of  $Y$ , and  $\alpha$  is the annealing operation:

$$\alpha = 1 - \left| \frac{n-1}{n} \right|^k \quad (21)$$

(3) At last, chaotic mutation variable  $W_i^{k*}$  is mapped to the feasible region, and thus complete a mutative operation.

$$W_i^k = a_i + (b_i - a_i) \cdot W_i^{k*} \quad (22)$$

$W_i^k$  is the chaotic value of the  $i$  th variables of  $W_i^k$ ,  $W^k = (W_1^k, W_2^k, \dots, W_n^k)$ .

#### i. AFSA- AL

This research presents an augmented Lagrangian methodology with a stochastic population based algorithm for solving nonlinear constrained global optimization problems. The method approximately solves a sequence of simple bound global optimization sub problems using a fish swarm intelligent algorithm. A stochastic convergence analysis of the fish swarm iterative process is included. Numerical results with a benchmark set of problems are shown, including a comparison with other stochastic-type algorithms [18].

The algorithm AFSA based on the augmented Lagrangian (AFSA AL) is presented below.

#### Algorithm 1. AFS aL Algorithm

**Given**  $\mu^+ > 0, 0 < \epsilon^* \ll 1, 0 < \alpha < 1, \gamma > 1, k_{\max}, 0 < \rho^- < \rho^+, \mu^1 \in [0, \mu^+]$ ;

**Step 1.** Randomly generate  $x^0$  in  $\Omega$ ;

**Step 2.** Compute  $\rho^1$  using (4), and set  $k = 1$ ;

**Step 3.** Repeat

{	<p>For a certain tolerance <math>\epsilon^k</math>, find an approximate minimizer <math>x^k</math> to the subproblem (3) using the AFS Algorithm;</p> <p>Update <math>\nu^k</math> using (5);</p> <p>If <math>k = 1</math> or <math>\ \nu^k\  \leq \alpha \ \nu^{k-1}\ </math> then</p> <p style="padding-left: 2em;"><math>\rho^{k+1} = \rho^k</math>;</p> <p>else</p> <p style="padding-left: 2em;">if <math>\ \nu^k\  \leq \epsilon^k</math> then</p> <p style="padding-left: 4em;"><math>\rho^{k+1} = \max\{\rho^-, \frac{1}{\gamma} \rho^k\}</math>;</p> <p style="padding-left: 2em;">else</p> <p style="padding-left: 4em;"><math>\rho^{k+1} = \min\{\rho^+, \gamma \rho^k\}</math>;</p> <p style="padding-left: 2em;">end if</p> <p>end if</p> <p>Update <math>\mu_i^{k+1} = \min\{\max\{0, \mu_i^k + \rho^k g_i(x^k)\}, \mu^+\}</math>, <math>i = 1, \dots, p</math>;</p> <p>Set <math>k = k + 1</math>;</p> <p>Until <math>\ \nu^{k-1}\  \leq \epsilon^*</math> or <math>k &gt; k_{\max}</math></p>
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The herein proposed technique for solving (3) uses a population-based algorithm that relies on swarm intelligence to converge towards the minimum value of the augmented Lagrangian function. This is the subject of the next section. Since the AFS algorithm provides a population of solutions,  $x^k$  is the best solution. We emphasize the importance of using  $x^k$  as one of the points of the population for the sub problem (3), at iteration  $k + 1$ . The remaining points of the population are randomly generated in the set  $\Omega$ .

#### j. AHSN-AFSA

The adaptive hybrid sequences niche artificial fish swarm algorithm (AHSN-AFSA) is introduced, and study on how to apply the algorithm to solve the vehicle routing problem. The concept of ecological niche is also being introduced in order to overcome the shortcoming of traditional artificial fish swarm algorithm to obtain optimal solution. Simulation results show that the new algorithm has solved fast, stable performance and so on [21].

#### k. TAFSA

In terms of some problems existing in the process of large case base retrieval, combining tabu search method and the advantages of artificial fish school algorithm, multilevel search strategy based on tabu artificial fish swarm algorithm. Tabu artificial fish swarm algorithm applies tabu table with a memory function to artificial fish swarm algorithm and uses different computing model in the similarity calculation according to properties of different types, effectively to avoid premature and blind search and other issues. Simulation results show that the algorithm outperforms other algorithms, it not only improves the retrieval accuracy and retrieval efficiency of the case based reasoning system, but also is characterized by requiring not much with the initial values and parameters, diversity search and overcoming the local maximum, better coordinate the overall and local search capabilities and provides an effective retrieval method to retrieve the case of large case base [23].

#### l. AFSA-FCM

This method applies the artificial fish swarm algorithm (AFSA) to fuzzy clustering. An improved AFSA with adaptive Visual and adaptive step is proposed. AFSA enhances the performance of the fuzzy C-Means (FCM) algorithm. A computational experiment shows that AFSA improved FCM outperforms both the conventional FCM algorithm and the Genetic Algorithm (GA) improved FCM [24].

##### l.1. ASFA fuzzy clustering approach

A new fuzzy clustering algorithm based on FCM and AFSA is proposed here. The algorithm has the following steps:

Step 1(Determine parameter encoding)

$V = (v_1, v_2, \dots, v_p, \dots, v_c)$  (Represents the centroid of the clusters. It is considered to be one AF.  $v_p$  is the centroid of the  $p^{th}$  cluster ( $1 \leq p \leq c$ ), where  $c$  is the number of clusters.  $V$  is a  $c*n$  dimension- vector.

**Step 2(Initialization)**

Define the clusters number  $c$ , the population of AF  $N$ , fuzziness exponent  $m$ , termination criterion, visual distance of AF, step of AF, crowd factor and Trynumber. Determine maximum iteration time  $K$  for AFSA, set iteration counter  $k=1$ ; initialize the first AF population:  $AF^K = \{V_1^K, V_2^K, \dots, V_q^K, \dots, V_N^K\}$  where  $V_q^K$ .

Represents the position of the  $q^{th}$  AF at the  $K^{th}$  iteration.  $1 \leq q \leq N$ ,  $N$  is the population of AF.

**Step 3(Global search)**

a) According to  $V_q^K$ , calculate membership matrix  $U_q^k = [u_{i,j}^k]_{c*n}$ .

b) Go to step 4 when the result satisfies the termination criterion, otherwise, increment  $k$  ( $k = k+1$ ) and go back to step 3(a).

**Step 4 (Local search)**

a) Find the best individual AF:  $V_{best}^k$

b) Calculate  $U^{K+1}$

c) Update  $V^{k+1}$

d) Stop iteration if the result satisfies termination criterion, or, increment  $k$  and return to step 4(b).

This algorithm is used to search for cluster centroid so that the objective function  $f$  is minimized. After each iteration, AFs swim to better locations. This enables convergence to the global optimum.

**m. HAFSA**

Based on particle swarm optimization (PSO) and artificial fish swarm algorithm (AFSA), a hybrid artificial fish swarm optimization algorithm is proposed. The novel method makes full use of the quickly local convergent performance of PSO and the global convergent performance of AFSA, and then is used for solving ill-conditioned linear systems of equations. Finally, the numerical experiment results show that the hybrid artificial fish swarm optimization algorithm owns a good globally convergent performance with a faster convergent rate. It is a new way for solving ill-conditioned linear systems of equations [25].

**n. NQAFSA**

Artificial Fish Swarm Algorithm (AFSA) is a new swarm intelligence optimization algorithm which is designed to find the single optimal solution for a given problem. But in some practical applications, the global optimal solution and some near optimal solutions are both needed. So a novel Niche Quantum Artificial Fish Swarm Algorithm (NQAFSA) is proposed in this method to solve these problems. The quantum mechanism is introduced into the AFSA to increase the diversity of species. Artificial Fish (AF) are divided into several sub-swarms to form the niche and the restricted competition selection (RCS) strategy is used to maintain the niche. The performance of NQAFSA is validated by the experimental results [26].

#### n.1. Niche Artificial Fish Swarm Algorithm based on Quantum theory

Niching techniques can find multiple solutions in multimodal domains, in contrast to AFSA that has been designed to locate only single optimal solution. A novel Niche Artificial Fish Swarm Algorithm based on Quantum theory called NQAFSA is proposed in this method. Quantum mechanism is introduced into AFSA so as to enhance population diversity and Niching technology is introduced into AFSA in order to find multiple optimal solutions. The probability amplitudes of quantum bits are employed to encode the position of the AF. The quantum rotation gate is used to update the position of the AF in order to enable the AF to move and the quantum non-gate is employed to realize the mutation of the AF for the purpose of speeding up the convergence.

The niche strategy is realized by the sub-swarm. The initial artificial fish swarm is split into smaller swarms as sub-swarm which is used to locate multiple solutions in multimodal function optimization problems. All the sub-swarm explores the search space in parallel way. The RCS strategy is employed to maintain the sub-swarm. The procedure of NQAFSA is shown as follows.

Step1. Initialization, including the number of sub-swarms  $N$ , the number of AF in each sub-swarm  $AF\_total$ ,  $AF\_step$ ,  $AF\_visual$ ,  $try\_number$ , mutation probability  $p_m$  and so on.

Step2. A total of  $N$  sub-swarms are created and they are all randomly distributed in the search space. The positions of AFs are encoded by the probability amplitudes of quantum bits.

Step3. Perform the solution space transformation for every AF in each sub-swarm and calculate fitness value of the AF, then the best AF in each sub-swarm will be included in the bulletin board of that sub-swarm.

Step4. AF execute  $AF\_Pray$ ,  $AF\_Swarm$ ,  $AF\_Follow$ ,  $AF\_Move$  and evaluate the results of the four behaviors. Then determine target position and change the position of the AF by quantum rotation gate.

Step5. Perform the mutation operation. Generate a random number  $rand_i$  between 0 and 1 for every AF, if  $rand_i < p_m$ , then execute mutation operation upon that AF.

Step6. Perform the solution space transformation for every AF and calculate fitness value of the AF again, then update the bulletin board in each sub-swarm.

Step7. The RCS strategy is executed to maintain the niche.

Step8. If the stopping criterion is satisfied, then stop and output the result; else go to Step4.

#### o. Hyperbolic Penalty in the Mutated Artificial Fish Swarm Algorithm

In this method the implementation of a population-based paradigm in the hyperbolic penalty function method to solve constrained global optimization problems is proposed. A mutated artificial fish swarm algorithm is used to solve the bound constrained sub problems. A simple tuning of the penalty parameters and three schemata for the implementation of an intensification local search procedure are introduced to promote convergence and improve the global solution. They may conclude that the proposed algorithm with an HJ intensification strategy outside the outer cycle provides promising results when solving engineering design problems. Future developments will focus on assigning different penalty parameters to each point of the population so that the level of infeasible penalization depends on the magnitude of constraint violation [27].

#### p. Parallel Fish Swarm Algorithm

With the development of Graphics Processing Unit (GPU) and the Compute Unified Device Architecture (CUDA) platform, researchers shift their attentions to general-purpose computing applications with GPU. In this method, they present a novel parallel approach to run artificial fish swarm algorithm (AFSA) on GPU. Experiments are conducted by running AFSA both on GPU and CPU respectively to optimize four benchmark test functions. With the same optimization performance, the running speed of the AFSA based on GPU (GPU-AFSA) can be as 30 time fast as that of the AFSA based on CPU (CPU-AFSA). As far as we know; this is the first implementation of AFSA on GPU [28].

#### q. QAFSA

In order to improve the global search ability and the convergence speed of the Artificial Fish Swarm Algorithm (AFSA), a novel Quantum Artificial Fish Swarm Algorithm (QAFSA) which is based on the concepts and principles of quantum computing, such as the quantum bit

and quantum gate is proposed in this method. The position of the Artificial Fish (AF) is encoded by the angle in  $[0, 2\pi]$  based on the qubit's polar coordinate representation in the 2-dimension Hilbert space. The quantum rotation gate is used to update the position of the AF in order to enable the AF to move and the quantum non-gate is employed to realize the mutation of the AF for the purpose of speeding up the convergence. Rapid convergence and good global search capacity characterize the performance of QAFSA. The experimental results prove that the performance of QAFSA is significantly improved compared with that of standard AFSA [29].

#### r. SA-AFSA

This method presents a novel stochastic approach called the simulated annealing-artificial fish swarm algorithm (SA-AFSA) for solving some multimodal problems. The proposed algorithm incorporates the simulated annealing (SA) into artificial fish swarm algorithm (AFSA) to improve the performance of the AFSA. The hybrid algorithm has the following features: the hybrid algorithm maintains 1) the strong local searching ability of the SA and 2) the swarm intelligence of AFSA. The experimental results indicate that in all the test cases, the SA-AFSA can obtain much better optimization precision and the convergence speed compared with AFSA [30].

## V. APPLICATION AFSA

The AFSA is a new and modern algorithm for optimization purposes. In short term it has succeeded to get its place among other optimization methods. Many researchers have applied this algorithm in different applications. In this section, its different applications are described.

#### a. Control

##### a.i. AFSA-FLC

This method provides an overview on the Artificial Fish Swarm Algorithm (AFSA) for the automated design and optimization of fuzzy logic controller. A new optimization method for fuzzy logic controller design is proposed. The membership functions of input and output variables are defined by six parameters, which are adjusted to maximize the performance of the controller by using AFSA. This method can improve the capability of search and convergence of algorithm. Simulation experiment on water level controller is discussed by using above method. The simulation results show that fuzzy logic controller based on AFSA avoids premature effectively and prove its feasibility [31].

#### a.ii. Self adaptive control algorithm of the artificial fish formation

With the deep study of swarm intelligence, biologists found that fish swarm changes in formation gradually in time during their movement. This formation change leads to a better and more effective access to evade predator and opportunity to capture food, so that the group's overall performance is improved. The architecture of artificial fish formation is established based on the behavioral model of artificial fish swarm. The mechanism of formation change is analyzed. A self-adaptive control algorithm of formation is proposed in this method. The parameters optimized PSO algorithm is used to simulate the process of keeping its balance during the formation change. Thus, the problem on relative bad adaptability and large systematic traffic in existing algorithms of formation is resolved [32].

#### a.iii. AFSA for Multi Robot Task Scheduling

The main aim of this study is managing robot tasks to minimize the deviation between the resource requirements and stated desirable levels. Some improved adaptive methods about step length are proposed in the Artificial Fish Swarm Algorithm (AFSA). In this study resource leveling methods are used to solve task scheduling problems in autonomous multi robot group. Robots are considered as resources. The experimental results show that proposed methods have better performances such as good and fast global convergence, strong robustness, insensitive to initial values, simplicity of implementation [33].

#### a.iv. AFSA in UCAV Path Planning

The path planning method based on artificial fish school algorithm (AFSA) was proposed to solve unmanned combat aerial vehicle (UCA V) path planning problem under the 2-D radar threats environment. According to the path planning requirements, the threat detection and artificial fish coding method were designed in detail. Besides, the method of perceiving threats was applied for advancing the feasibility of the path. A comparison of the results was made by WPSO, CFPSO and AFSA, which showed that the method we proposed in this paper was effective. AFSA was much more suitable for solving this kind of problem [34].

#### a.v. AFSA for Fault Diagnosis in Mine Hoist

It has been presented an intelligent methodology for diagnosing incipient faults in mine hoist. As Probabilistic Causal-effect Model-Based diagnosis is an active branch of Artificial Intelligent, the feasibility of using probabilistic causal-effect model is studied and it is applied

in artificial fish-swarm algorithm (AFSA) to classify the faults of mine hoist. In probabilistic causal-effect model, we employed probability function to nonlinearly map the data into a feature space, and with it, fault diagnosis is simplified into optimization problem from the original complex feature set. And an improved distance evaluation technique is proposed to identify different abnormal cases. The proposed approach is applied to fault diagnosis of friction hoist with many steel ropes, and testing results show that the proposed approach can reliably recognize different fault categories.

Moreover, the effectiveness of the method of mapping hitting sets problem to 0/1 integer programming problem is also demonstrated by the testing results. It can get 95% to 100% minimal diagnosis with cardinal number of fault symptom sets greater than 20 [35].

#### a.vi. CAFAC

Efficient identification and control algorithms are needed, when active vibration suppression techniques are developed for industrial machines. A new actuator for reducing rotor vibrations in electrical machines is investigated. Model-based control is needed in designing the algorithm for voltage input, and therefore proper models for the actuator must be available. In addition to the traditional prediction error method a new knowledge-based Artificial Fish-Swarm optimization algorithm (AFA) with crossover, CAFAC, is proposed to identify the parameters in the new model. Then, in order to obtain a fast convergence of the algorithm in the case of a 30kW two-pole squirrel cage induction motor, they combine the CAFAC and Particle Swarm Optimization (PSO) to identify parameters of the machine to construct a linear time-invariant (LTI) state-space model. Besides that, the prediction error method (PEM) is also employed to identify the induction motor to produce a black box model with correspondence to input-output measurements [36].

#### a.vii. MOAFSA

Artificial Fish Swarm Algorithm (AFSA) is a kind of swarm intelligence algorithm, which has the features of fast convergence, good global search capability, and strong robustness and so on. An approach using AFSA to solve the multiobjective optimization problem is proposed. In this algorithm, the concept of Pareto dominance is used to evaluate the pros and cons of Artificial Fish (AF). Artificial fish swarm search the solution space in parallel and External Record Set is used to save the found Pareto optimal solutions. The simulation results of 4 benchmark test functions illustrate the effectiveness of the proposed algorithm [37].

#### a.viii. PID Controller Parameters Based on an Improved AFSA

The artificial fish swarm algorithm is a new kind of optimizing method based on the model of autonomous animals. After analyzing the disadvantages of AFSA, an improved artificial fish swarm algorithm is presented. According to the ergodicity and stochasticity of chaos, the basic AFSA is combined with chaos in order to initialize the fish school. The improvement of the swarming behavior increased the precision of the algorithm. In the behavior of preying, the strategy of dynamically adjusting the parameter of step is presented in order to improve the convergence rate of the algorithm. This improved AFSA is applied in the optimization of the of PID controller parameters. The simulation results show that this improved AFSA algorithm is effective and better than the basic AFSA algorithm [38].

#### a.ix. Optimum steelmaking charge plan using AFSA

An optimum furnace charge plan model for steelmaking continuous casting planning and scheduling is presented an artificial fish swarm optimization (AFSO) algorithm is used to solve the optimum charge plan problem. The computation with practical data shows that the model and the solving method are very effective [39].

#### a.x. AFSA for the Target Area on Simulation Robots

In this research, they used an improved algorithm of artificial fish, and did the optimization in setting the border in the simulation platform, especially in the field of choosing ways of the robots; they used the Multi-threshold to reduce the uncontrollable actions when robots are in the game. And this method gives them an acceptable way to solve the issue [40].

### b. Image processing

#### b.i. AFSA-Kmeans

Data clustering has been used in different fields such as machine learning, data mining, wireless sensory networks and pattern recognition. One of the most well-known clustering methods is K-means which has been used effectively in many of clustering problems. But this algorithm has problems such as convergence in local minimum and sensitivity to initial points. A hybrid clustering method, based on artificial fish swarm optimization (AFSO) and K-means so called KAFSO is proposed. In this proposed algorithm, high ability of AFSO in global searching as well as high ability of K-means in local searching has been used cooperatively. The proposed method has been tested on eight collections of standard data and its efficiency has been compared with standard methods PSO, Kmeans, K-PSO and AFSO.

Experimental results showed that proposed approach has suitable and acceptable efficacy in data clustering [42].

#### b.ii. HA-FC

In CBR system, the case base is becoming increasingly larger with the incremental learning which results in the decline of case retrieval efficiency and its weaker performance. Aiming at such weakness of CBR system, a novel case retrieval method based on Hybrid Ant-Fish Clustering Algorithm (HA-FC). At beginning of algorithm, we get rough cluster sets utilizing the advantage of Artificial Fish-school Algorithm which is insensitive to initial value and has high speed of searching optimizing. Then they used ant Colony Optimization introduced the concept of Crowded Degree to avoid convergence too early and improve the ability of searching optimizing. Finally, apply this algorithm to case retrieval in order to reduce searching time and improve searching accuracy. The results of simulation demonstrate the effectiveness of this algorithm [43].

#### b.iii. A Clustering Algorithm Based on Artificial Fish School

For avoiding the dependence of the validity of clustering on the space distribution of high dimensional samples of Fuzzy C2Means, a dynamic fuzzy clustering method based on artificial fish swarm algorithm was proposed By introducing a fuzzy equivalence matrix to the similar degree among samples, the high dimensional sample  $s$  were mapped to two dimensional planes. Then the Euclidean distance of the samples was approximated to the fuzzy equivalence matrix gradually by using artificial fish warm algorithm to optimize the coordinate values. Finally, the fuzzy clustering was obtained. The proposed method, not only avoided the dependence of the validity of clustering on the space distribution of high dimensional samples, but also raised the clustering efficiency. Experiment results show that it is an efficient clustering algorithm [41].

For clusters of individual fish behavior in the initial state for the  $X_i$ , any exploration of a state  $X_j$ , calculate  $d_{ij}$  and  $d_{ij} = || X_i - X_j ||$ , if  $j$ 's position is not too crowded place  $i$  move to  $j$ , otherwise implementation of the foraging behavior and foraging behavior of the state is a random choice, so difficult in the short time between the individual fish to find categories. If the initial heuristic is given when the amount of information that can further enhance the convergence speed.

The specific steps the algorithm Based cluster analysis of the data set is  $X = (X_i = (x_{i1} x_{i2} \dots, x_{in}), i = 1, 2, \dots, n)$ , concrete steps are as follows:

- a)  $n = 0$  ( $n$  is number of cycles), given the variables in fish (biscual, step,) the initial value and the current state of the AF\_X.
- b) First for fast classification, the classification results calculated according to the cluster center  $Z_j$  ( $j = 1, 2, \dots, K$ ).
- c) the current status of individual fish,  $X_i$ , calculated with center  $Z_j$  ( $j = 1, 2, \dots, K$ ). Distance, if its not too crowded neighborhood of the center is moving toward the center.
- d) Otherwise, the best neighborhood to find  $X_i$  neighbor  $X_{max}$ . If the food is rich in not too crowded to its direction.
- e) In two steps do not meet their perception in the context of the election of a state, if the location of the food concentration is high then its direction.
- f)  $n = n + 1$ , if  $n$  is greater than the number required to stop operation, output the best solution. Otherwise transfer step (2) to continue. Diagram in Fig.2 below.

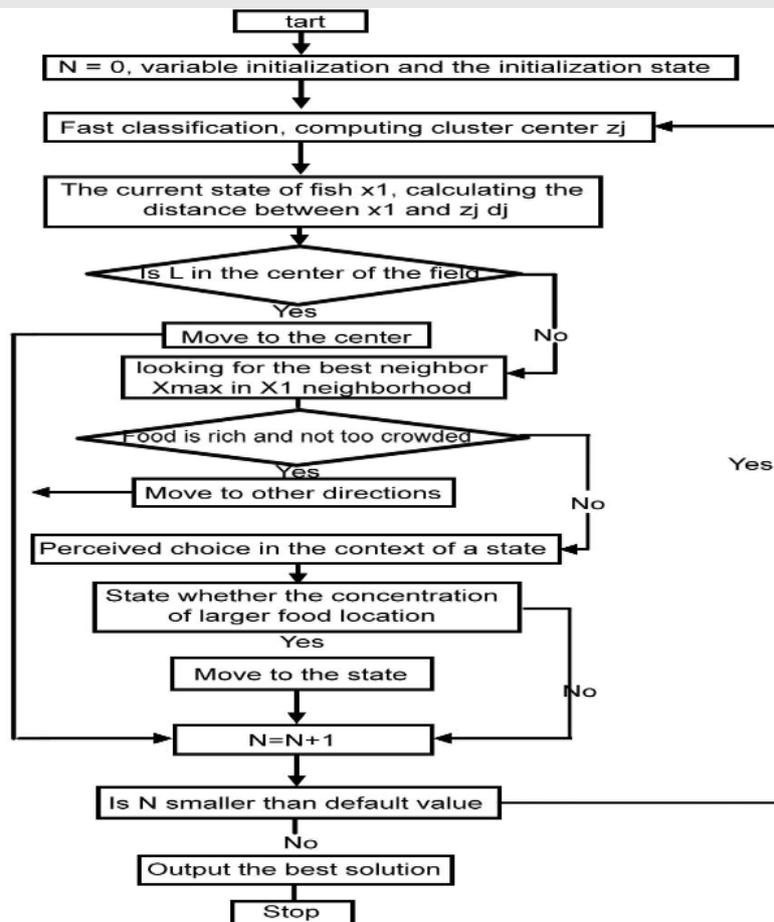


Figure 2 .clustering algorithm based on artificial fish flow

#### b.iv. Image Reconstruction Algorithm Based on AFS for ECTS

According to the fundamental principles of electrical capacitance tomography (ECT), a new ECT algorithm optimized Radial Basis Function (RBF) neural network algorithm, which is based on Artificial Fish Swarm Algorithm (AFSA), is proposed against the “soft field” effects and ill-conditioning problems in ECT technology. After giving the mathematic model of the algorithm, this research also applies the AFSA to the training process of neural networks to compare with the traditional neural network algorithm. At last, a conclusion that with little error, high quality and fast convergence rate, etc. The ECT image reconstruction algorithm which is based on AFSA and the optimized RBF neural networks providing a new way for the ECT image reconstruction algorithm is reached [44].

#### b.v. Artificial Fish - Fuzzy C-Means Clustering Algorithm

By analyzing advantages and disadvantages of Fuzzy C-Means Clustering Algorithm, a method of image segmentation based on Fuzzy C-Means Clustering Algorithm and Artificial Fish Swarm Algorithm is proposed. The image is segmented in terms of the values of the membership of pixels, Artificial Fish Swarm Algorithm is introduced into Fuzzy C-Means Clustering Algorithm, and through the behavior of prey, follow, swarm of artificial fish, the optimized clustering center could be selected adaptively, then the values of the membership of pixels available with Fuzzy C-Means Clustering Algorithm, and the image segmentation is completed. The experimental results show the effectiveness and feasibility [45].

#### b.vi. IAFSC

An improved artificial fish swarm algorithm (IAFSA) is proposed, and its complexity is much less than the original algorithm (AFSA) because of a new proposed fish behavior. Based on IAFSA, two novel algorithms for data clustering are presented. One is the improved artificial fish swarm clustering (IAFSC) algorithm, the other is a hybrid fuzzy clustering algorithm that incorporates the Fuzzy C-means (FCM) into the IAFSA. The performance of the proposed algorithms is compared with that of the Particle Swarm Optimization (PSO), K-means and FCM respectively on Iris testing data. Simulation results show that the performance of the proposed algorithms is much better than that of the PSO, K-means and FCM. And the proposed hybrid fuzzy clustering algorithm avoids the FCM’s weakness such as initialization value problem and local minimum problem [46].

#### b.vii. IAFSA – Segmentation

An improved artificial fish swarm algorithm is proposed to search the optimal parameter combination in this method. It is concerned with fuzzy entropy definition used for image segmentation. The key problem associated with this method is to find the optimal parameter combination of membership function so that an image can be transformed into fuzzy domain with maximum fuzzy entropy. Then, they compare the improved artificial fish swarm algorithm with other artificial intelligence models. The experiment indicates that the proposed method is quite effective and ubiquitous [47].

#### b.viii. CQAFSA

Color quantization (CQ) is one of the important techniques in image compression, graphic and image processing. Most of quantization methods are based on clustering algorithms. Data clustering is a non-supervised classification technique and belongs to NP-hard problems. One of the methods for solving NP-hard problems is applying swarm intelligence algorithms. Artificial fish swarm algorithm is one of the swarm intelligence algorithms which is working based on population and random search. In this research, a modified AFSA is proposed for doing CQ. In the proposed algorithm, to improve the efficiency and remove AFSA weaknesses, some modifications are done on behaviors, parameters and the algorithm procedure. The proposed algorithm along with other multiple known algorithms has been used on some famous images for doing CQ. Experimental results comparison shows that the proposed algorithm has acceptable efficiency [48].

#### c. Network

##### c.i. WSN-AFSA

Wireless sensor networks (WSN) will enable the reliable monitoring of a variety environment for both civil and military applications. These networks require robust wireless communication protocols for the purpose of balancing the load and prolonging the network lifetime. In this method, they propose a novel hierarchical routing protocol based on artificial fish swarm optimization (AFSO). Utilizes AFSO algorithm in cluster formation phase, its main object is to solve the NP-hard problem of finding  $k$  optimal clusters according to the given rules. The performance of the novel protocol is compared with the well known cluster-based protocol LEACH and LEACH-C. As the experiment results shown, the protocol can not only improve system lifetime but also prevent the networks form seriously energy consumption [49].

#### c.ii. The hybrid algorithm based on fish and particle swarm algorithm

The coverage problem is one basic problem in the wireless sensor networks (WSNs). In one limited region, how to reasonably arrange the sensor nodes to achieve the best coverage is the key to improve the performance of the whole networks. a hybrid algorithm which is based on the fish swarm algorithm and particle swarm optimization in the limited WSNs region. The new algorithm has the well global search ability of the fish swarm algorithm and the quickly search ability of the particle swarm optimization. The simulation results show that the hybrid algorithm can effectively optimize the nodes' deployment of the sensor networks to improve the coverage of the whole networks [50].

#### c.iii. AFSA in Intrusion Detections

A method of optimization and simplification to network feature using Artificial Fish-swarm Algorithm in intrusion detection is proposed in this method for solving problems of more features and slower computing speed. This method established mathematic model aimed at achieving higher detection rate and lower false positive rate, and obtaining optimal feature attributes through iterative method by using an optimization policy on the basis of "PREY, SWARM and FOLLOW" operators. 41 features are optimized and simplified by adopting this method. 31% feature attributes are achieved, which can completely reflect intrusion feature. The experimental results show that using feature attributes after optimization and simplification can shorten 40% work time in intrusion detection [51].

#### c.iv.QoS-AFSA

Bandwidth-delay-constrained multicast routing problem is an NP-complete problem. a QoS multicast routing algorithm based on Artificial Fish Swarm optimization. Meeting with the Bandwidth-delay constrained, the proposed algorithm can search the least-cost multicast routing tree quickly. Simulation results show that this algorithm has high reliability and good performance of global optimization, and suit for real-time, high-speed multimedia transmission network [52].

#### c.v. IMAFSA

The hybrid artificial fish swarm optimization algorithm based on mutation operator and simulated annealing algorithm (MAFSA) is studied and improved. The mutation operator was improved and a method for tentative determining of mutation probability was presented in improved MAFSA (IMAFSA). Besides, economic and security objective function is also

applied to improve the model of reactive power optimization of distribution network. The result obtained from simulated calculation in real distribution network shows that the IMAFSA applied in reactive power optimization of distribution network is reasonable and feasible [53].

#### c.vi. IAFSO-IECBP

IEC three-ratio is an effective method for transformer fault diagnosis in the dissolved gas analysis (DGA). Considering the characteristic of three-ratio boundary is too absolute, fuzzy knowledge is utilized to preprocess. As the same time, for overcoming the deficiency of the back propagation (BP), an improved artificial fish swarm optimization (IAFSO) algorithm is used to optimize the weight and threshold of the BP. The global searching ability of the IAFSO approach is utilized to find the global optimization solution. It can overcome the slower convergence velocity and easily getting into local extremum of the BP neural network. So, aiming at the shortcoming of BP neural network and three ratios, blurring the boundary of the gas ratio and the IAFSO algorithm is introduced to optimize the BP network. Then the IAFSO-IECBP method is proposed. Experimental results indicate that the proposed algorithm in this method that both convergence velocity and veracity are all improved to some extent. Correctness and validity of this proposed method has also confirmed for transformer fault diagnosis [54].

#### d. Neural Network

##### d.i. NNC-AFSA

As a novel simulated evolutionary computation technique, Artificial Fish Swarm Algorithm (AFSA) shows many promising characters. The use of AFSA as a new tool which sets up a neural network (NN), adjusts its parameters, and performs feature reduction, all simultaneously. In the optimization process, all features and hidden units are encoded into a real-valued artificial fish (AF), and give out the method of designing fitness function. The experimental results on several public domain data sets from UCI show that our algorithm can obtain an optimal NN with fewer input features and hidden units, and perform almost as good as even better than an original complex NN with entire input features. And also indicate that optimizing a network classifier for a specific task has the potential to produce a simple classifier with low classification error and good generalization ability [55].

##### d.ii. Forecasting stock indices using RBFNN by AFSA

Stock index forecasting is a hot issue in the financial arena. As the movements of stock indices are nonlinear and subject to many internal and external factors, they pose a great challenge to researchers who try to predict them. They select a radial basis function neural network (RBFNN) to train data and forecast the stock indices of the Shanghai Stock Exchange. They introduce the artificial fish swarm algorithm (AFSA) to optimize RBF. To increase forecasting efficiency, a K-means clustering algorithm is optimized by AFSA in the learning process of RBF. To verify the usefulness of our algorithm, they compared the forecasting results of RBF optimized by AFSA, genetic algorithms (GA) and particle swarm optimization (PSO), as well as forecasting results of ARIMA, BP and support vector machine (SVM). Their experiment indicates that RBF optimized by AFSA is an easy-to-use algorithm with considerable accuracy. Of all the combinations we tried in this method, BIAS6 + MA5 + ASY4 was the optimum group with the least errors [56].

#### d.iii. Freight Prediction Based on BPNN Improved by CAFSA

Back Propagation (BP) neural network has widely application because of its ability of self-studying, self-adapting and generalization. But there are some intrinsic defaults, such as low convergence speed, local extremes and so on. Artificial fish swarm algorithm (AFSA) is an up-to-date proposed optimal strategy, which possesses good capability to avoid the local extremum and obtain the global extremum. In order to improve the search efficiency of AFSA, Chaos system is introduced. A quantitative forecast method based on the BP network improved by Chaos artificial fish-swarm algorithm is proposed in the paper. The model is trained with the freight data of a city and then used to forecast the freight. Compared the simulated results with BP network and BP network improved by other algorithm, it concludes that CAFSA-BPN has smaller error in forecasting. And it indicates that CAFSA has the capability of fast learning the weight of network and globally search, and the training speed of the improved BP network is greatly raised [57].

#### d.iv. RF-AFSA for short time Forecast of Stock Indices

The movement of stock index is difficult to predict for it is non-linear and subject too many inside and outside factors. Researchers in this field have tried many methods, SVM and ANN, for example, and have achieved good results. In this method, they select Radial Basis Functions Neural Network (RBFNN) to train data and forecast the stock index in Shanghai Stock Exchanges. In order to solve the problem of slow convergence and low accuracy, and to ensure better forecasting result, they introduce Artificial Fish Swarm Algorithm (AFSA) to

optimize RBF, mainly in parameter selection. Empirical tests indicate that RBF neural network optimized by AFSA can have ideal result in short-term forecast of stock indices [58].

#### d.v. Time Series Forecasting on Novel SVM Using AFSA

Time series analysis is an important and complex problem in machine learning. Support vector machine (SVM) has recently emerged as a powerful technique for solving problems in regression, but its performance mainly depends on the parameters selection of it. Parameters selection for SVM is very complex in nature and quite hard to solve by conventional optimization techniques, which constrains its application to some degree. Artificial Fish Swarm Algorithm (AFSA) is proposed to choose the parameters of least squares support vector machine (LS-SVM) automatically in time series prediction. This method has been applied in a real Electricity Load Forecasting, the results show that the proposed approach has a better performance and is also more accurate and effective than LS-SVM based on particle swarm optimization [59].

#### e. Scheduling

##### e.i. IAFSA-RL

An overview on the Artificial Fish Swarm Algorithm (AFSA) for the resource leveling .Some improved adaptive methods about step length are proposed in the AFSA. This method have better performances such as good and fast global convergence, strong robustness, insensitive to initial values, simplicity of implementation. The simulation results show that the resource leveling based on AFSA avoids premature effectively and prove its feasibility [60].

The planning and implementation of power plant project have the characters of “within long period, large Resource devotion and resource imbalance”. Project resource distribution is not an ideal state, but is “multi peak” and “multi-valley”. This imbalance increases investment risks, which may cause waste of resources. Therefore, it is urgently necessary to make a reasonable adjustment in the network planning process in order to achieve a balanced allocation of resources and to solve the problems. Resource leveling can be classified into a mathematical model with a class of nonlinear programming, but there are imitations in study. In large scale networks, the CPU time for solving such problems increases exponentially with the rising of the number of network nodes. As for different network structures and different parameters, the influence on resources leveling is not the same. Network parameters can be considered as AF. The improved AFSA algorithm considers about the optimal individual, and the weighted processing identifies Global optimal program. It avoids the process of

optimization in a “local optimization, and global nongifted” result. Therefore, the application of AFSA in resources leveling can extend profound manifestation of the superiority of the algorithm.

#### e.ii. Efficient Job Scheduling in Grid Computing with MAFSA

One of the open issues in grid computing is efficient job scheduling. Job scheduling is known to be NP-complete, therefore the use of non-heuristics is the de facto approach in order to cope in practice with its difficulty. A modified artificial fish swarm algorithm (MAFSA) for job scheduling. The basic idea of AFSA is to imitate the fish behaviors such as preying, swarming, and following with local search of fish individual for reaching the global optimum. The results show that our method is insensitive to initial values, has a strong robustness and has the faster convergence speed and better estimation precision than the estimation method by Genetic Algorithm (GA) and simulated annealing (SA) [61].

#### e.iii. Multi-Robot Task Allocation and Scheduling based on FSA

The problem of multi robot task allocation and scheduling is to assign more relative tasks to less relative robots and to scheme task processing sequence so as to minimize the processing time of these tasks. The key of this problem is to allocate proper quantity of tasks for each robot and schedule the optimal task sequence for each robot. In order to minimize the processing time for robots, an optimized multiple robots task allocation and scheduling approach based on fish swarm algorithm is proposed. In this approach, the optimized task sequence is first schemed using fish swarm algorithm on the assumption that all the tasks are processed by one robot. Then, according to the number of the robots, the task sequence has been randomly divided into several task segments that will be assigned to robots. At last, the task numbers of each task segments are averaged according to the time each robot used, therefore proper quantity of tasks is allocated to each robot and the optimized task allocation scheme is got. To validate the effectiveness of the proposed approach, experiments and simulation have been made. The results show that the proposed approach can scheme optimized multi robots task allocation and scheduling scheme [62].

#### e.iv. Scheduling Arrival Aircrafts on Multi-runway Based on an IAFSA

The aircraft landing scheduling (ALS) problem is a typical NP-hard optimization problem. Based on an improved artificial fish swarm algorithm (IAFSA), the problem of scheduling arrival aircrafts at an airport with multi-runway is studied. A mutation operator is introduced

to the artificial fish swarm algorithm. The sequence problem of landing aircraft is solved, and the simulation result shows that the IAFSA of ALS is better than FCFS which can decrease the total delay time by 24.1%. This method can obtain a satisfactory solution which can provide real-time support for automatic air traffic management [63].

#### f. Signal processing

##### f.i. A Weak Signal Detection Method Based on AFSA Matching Pursuit

To detect weak signals is difficult in signal processing and is very important in many areas such as non-destructive evaluation (NDE), radar etc. Sparse signal decomposition from over complete dictionaries is the most recent technique in the signal processing community. In this paper, this technique is utilized to cope with ultrasonic weak flaw detection problem. But its calculation is huge (NP problem). A new improved matching pursuit algorithm is proposed. The mathematical model of searching algorithms based on artificial fish swarm is established; the artificial fish swarm with the advantages of distributed parallel searching ability, strong robustness, good global astringency, and insensitive preferences are employed to search the best matching atoms. It can reduce complexity of sparse decomposition and space of memory. Experimental results shows that the amplitude, frequency and initial phase parameters of ultrasonic signal blurred by strong noise can be estimated according to the proposed algorithm and the expected weak signal can be then reconstructed. When this method is used in the ultrasonic flaw detection, compared with the wavelet entropy and wavelet transform, the results show that the signal quality and performance parameters are improved obviously [64].

##### f.ii. Wavelet Threshold optimization with AFSA

AFSA is a new intelligent optimization algorithm based on animal's behaviors. This algorithm can be used to the solution of global optimization problems and is an application prototype of swarm intelligent optimization problem. It uses the animal bottom behavior process, and finds the global optimum through the individual's local optimization. Signal processing involves many optimization problems, and we can reduce the processor (storage resource) or enhance the effect of signal processing by optimization. Here they obtain the optimal wavelet denoising threshold using the new optimization algorithm-AFSA [65].

## VI. CONCLUSIONS

The AFSA algorithm is one of the most appropriate methods for swarm intelligence optimization. This algorithm is capable of solving the problems by inspiration from the en

masse movement of fishes. Fishes show different behaviors including seeking for food, following other fishes, protecting the group against threats and stochastic search. These behaviors have been employed in the AFSA and an acceptable result has been obtained. This algorithm shows more intelligent behavior and obtains more optimized results compared with other swarm intelligence algorithms. Of course, this algorithm has some disadvantages like falling in local optimum points, advanced convergence and time consuming. This algorithm is one of the best approaches of the Swarm Intelligence method with considerable advantages like high convergence speed, flexibility, error tolerance and high accuracy. this paper review the AFSA algorithm, its evolution stages from the start point up to now, improvements and applications in various fields like optimization, control, image processing, data mining, improving neural networks, networks, scheduling, and signal processing and so on. Also, various methods combining the AFSA with other optimization methods like PSO, Fuzzy Logic, Cellular Learning Automata or intelligent search methods like Tabu search, Simulated Annealing , Chaos Search and etc. This algorithm has been widely used in short time and we hope the researchers can improve it more.

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